

# Inferring the seizure propagation patterns using a data-driven model of a threshold network

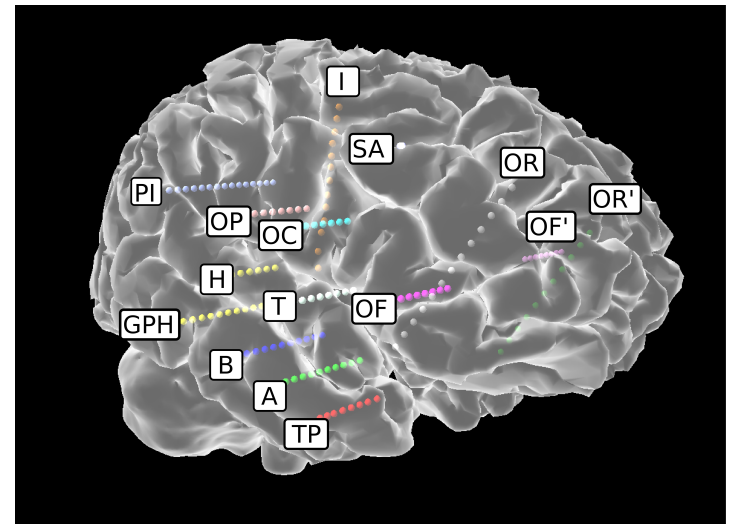
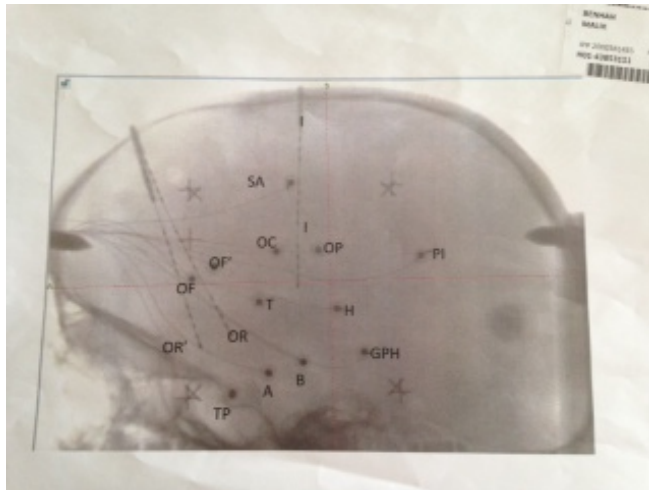
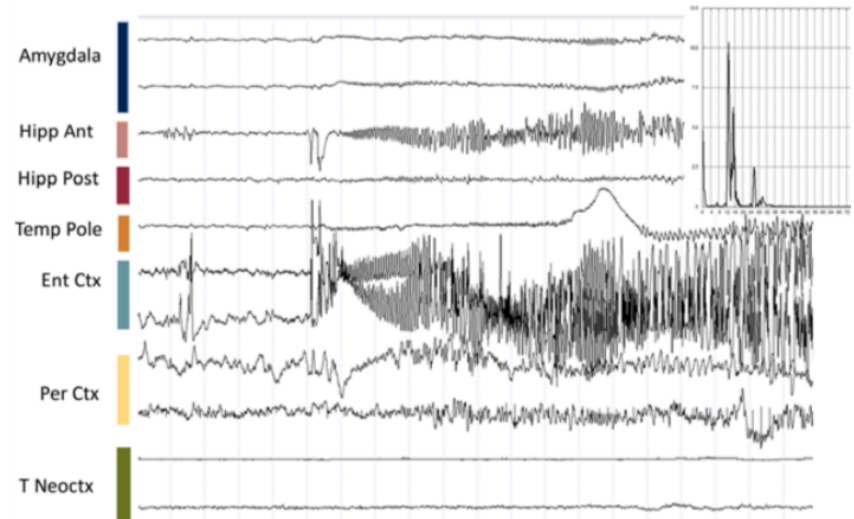
Viktor Sip

Institut de Neurosciences des Systèmes  
Aix-Marseille Université

Threshold Networks, 22 - 24 July, Nottingham

# Epilepsy

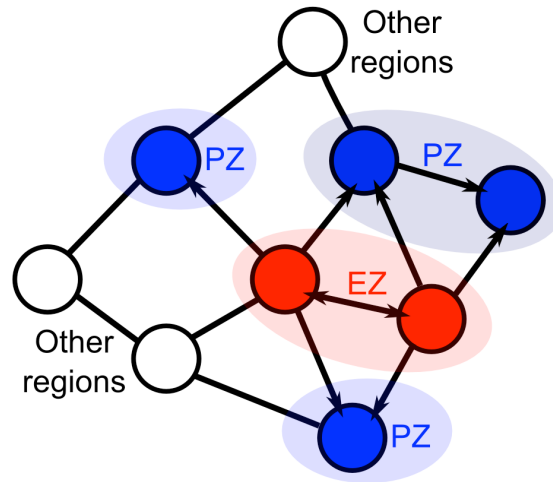
- During focal epileptic seizures, abnormal electrical activity spreads through the brain network.
- Intracranial electroencephalography is used to observe the activity.
- Whole network cannot be observed (subsampling problem).



Bartolomei et al. Brain (2017)

# Epileptogenic zone

- “The site of the beginning of the epileptic seizures and of their primary organization.” (Talairach, Bancaud 1965)
- “The area of cortex that is necessary and sufficient for initiating seizures and whose removal is necessary for complete abolition of seizures.” (Luders 1993)

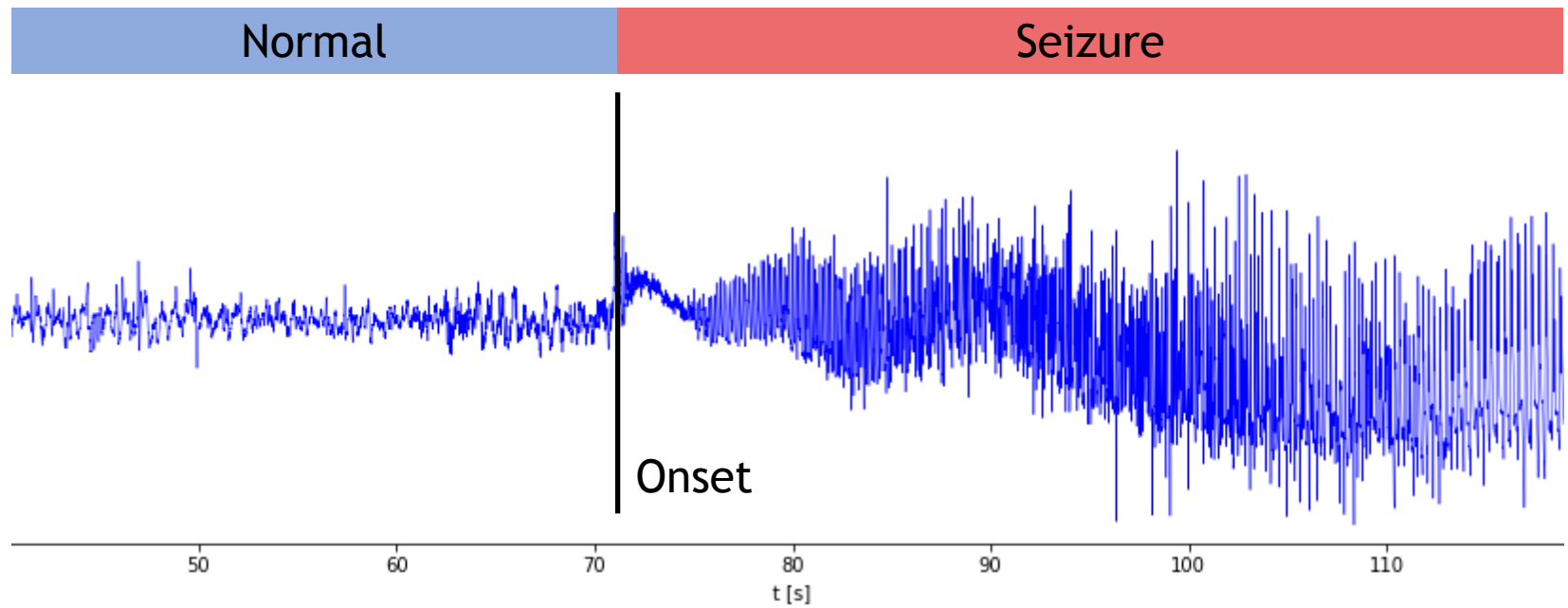


EZ: Epileptogenic zone  
PZ: Propagation zone

Jirsa et al, NeuroImage (2016)

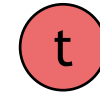
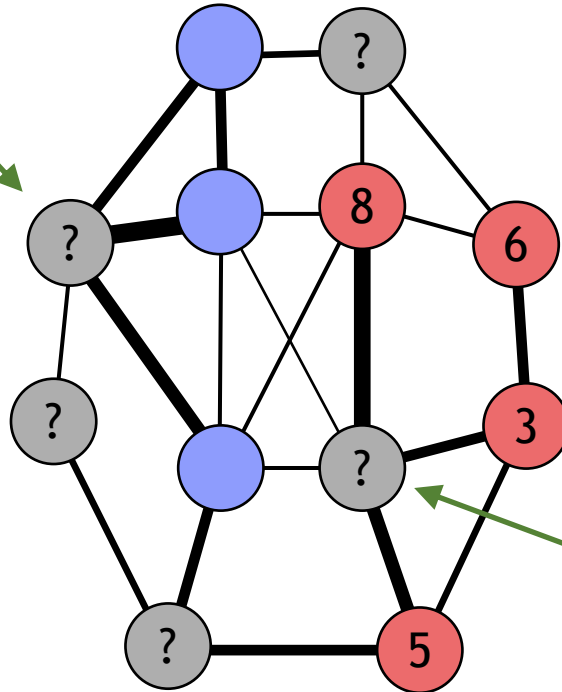
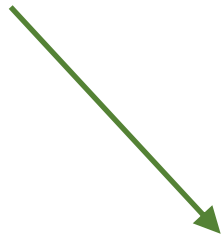
- Surgery success rate around 60 - 70%.

# Normal and seizure activity

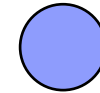


# Conceptual view

Probably non-seizing



Region seizing at time  $t$



Non-seizing region



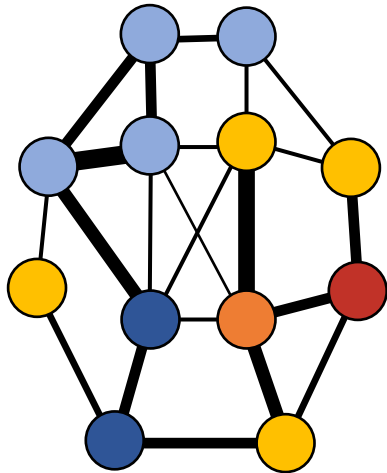
Hidden region

Probably seizing

**Goal:** To infer what happens in the hidden regions.

# Conceptual view

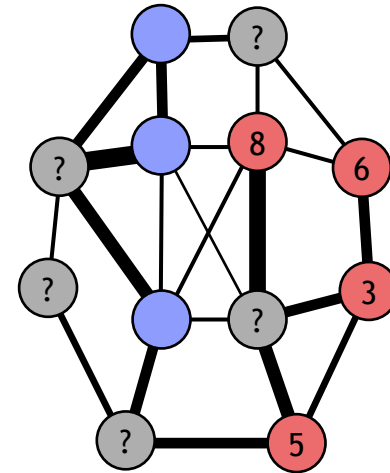
Structure (known)  
+ excitabilities (unknown)



Propagation  
dynamics  
(unknown)



Onset times (partially known)



- Data: structural and functional data from tens of subjects
- Assumption: Propagation dynamics is shared among subjects

# Threshold model of seizure propagation

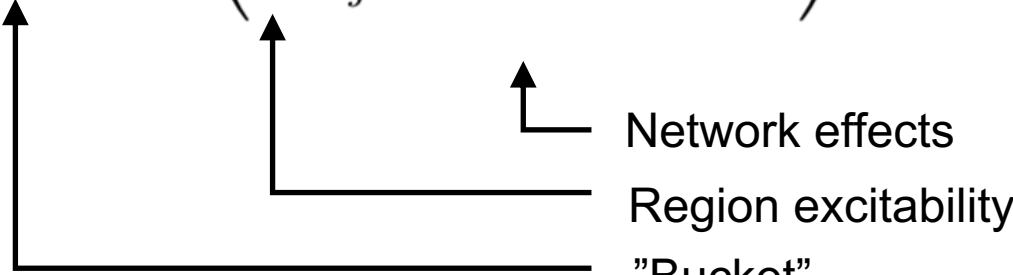
$$\dot{z}_i = f_{\mathbf{q}} \left( c_i, \sum_{j=1}^n w_{ij} H(z_j - 1) \right), \quad z_i(0) = 0$$


Diagram illustrating the components of the equation:

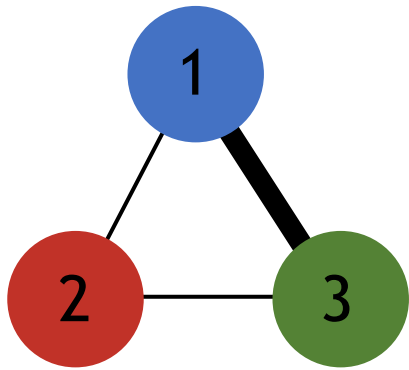
- "Bucket" points to  $c_i$
- Region excitability points to  $\sum_{j=1}^n w_{ij} H(z_j - 1)$
- Network effects points to  $f_{\mathbf{q}}$

Function  $f_{\mathbf{q}}$  :

- Positive
- Increasing in the first variable
- Parameterized by vector  $\mathbf{q}$

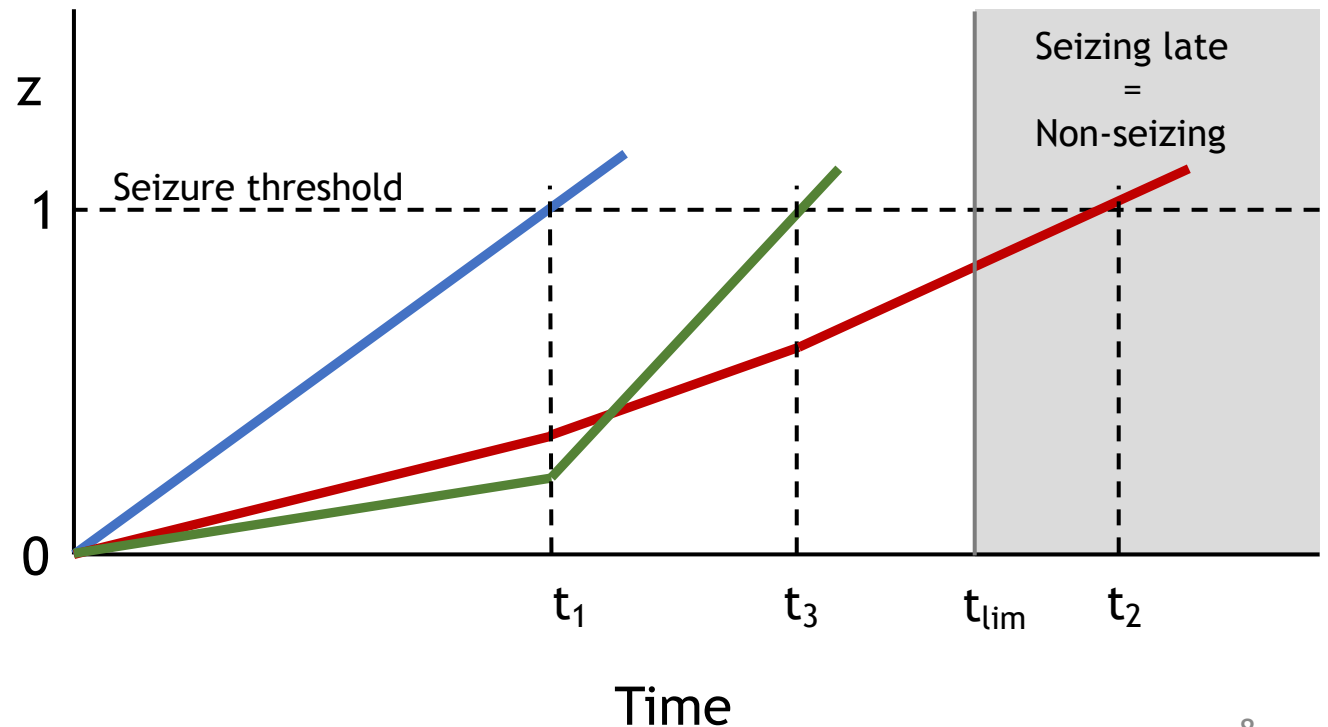
# Threshold model of seizure propagation

$$\dot{z}_i = f_{\mathbf{q}} \left( c_i, \sum_{j=1}^n w_{ij} H(z_j - 1) \right), \quad z_i(0) = 0$$



Excitability:

$$c_1 > c_2 > c_3$$





# Bayesian inference

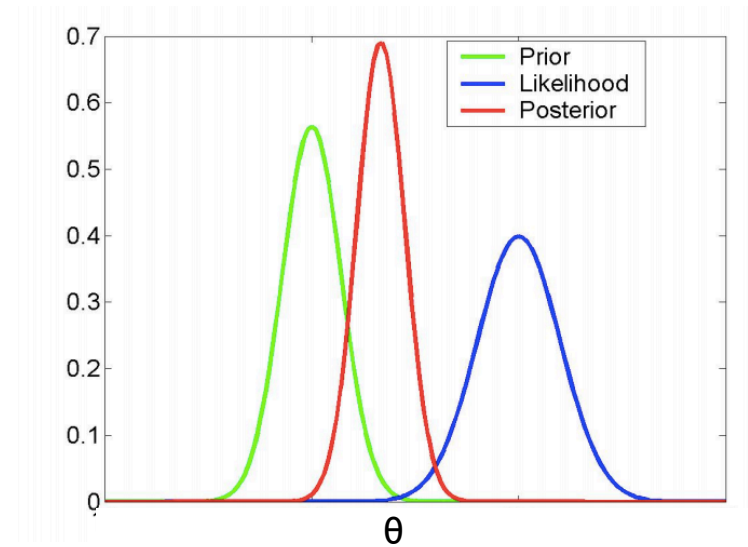
$$p(\theta \mid D) = \frac{p(D \mid \theta)p(\theta)}{\int p(D, \theta)d\theta}$$

posterior

Likelihood

prior

Marginal likelihood  $p(D)$   
(model evidence)



Thomas Nichols: Bayesian inference

D ... observed data

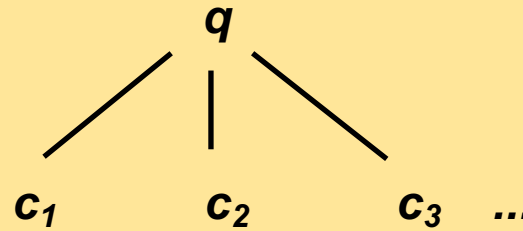
$\theta$  ... unknown parameters

# Hierarchical model

## Parameters

Hyperparameters (4)

Seizure-specific excitabilities  
( $n_{\text{seizures}} \times n_{\text{regions}}$ )



Non-informative prior

$N(0, 1)$

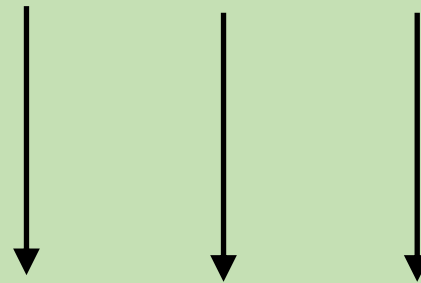
PRIOR

## Connectome matrices

$W_1$     $W_2$     $W_3$  ...

## Dynamical model

$$\dot{z}_i = f_q \left( c_i, \sum_{j=1}^n w_{ij} H(z_j - 1) \right)$$



LIKELIHOOD

## Observations

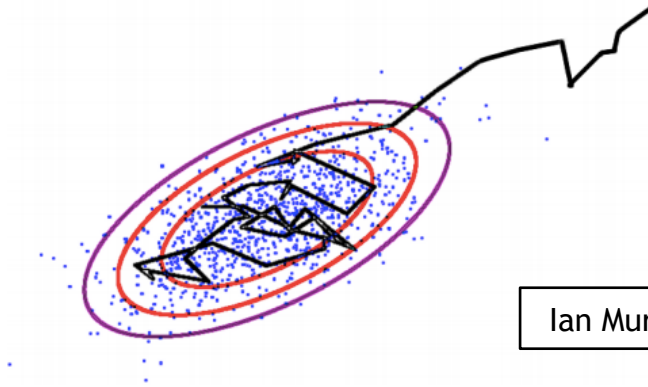
- Seizing/non-seizing regions
- Onset times

$obs_1$     $obs_2$     $obs_3$  ...

# Sampling from the posterior

## Markov Chain Monte Carlo (MCMC):

Build a Markov chain whose steps approximate the posterior distribution.



Ian Murray: Advanced MCMC methods (2006)

## Metropolis-Hastings:

- Random walk + acceptance probability

## Hamiltonian Monte Carlo (HMC):

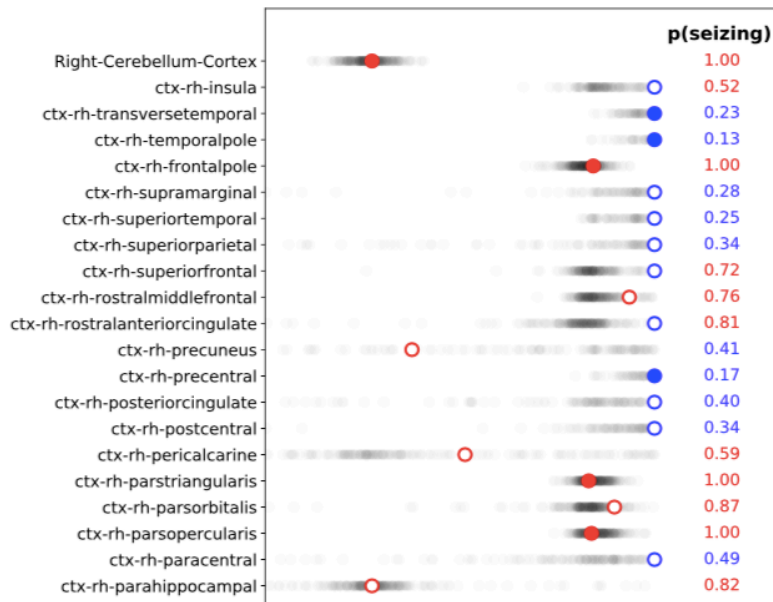
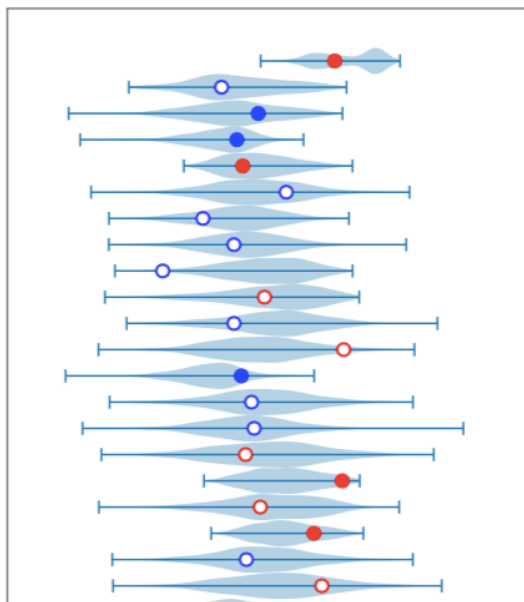
- MCMC method using the potential and kinetic energy to explore the posterior distribution.
- More efficient for complicated geometries in high dimensional spaces

# Validation with synthetic data

- Realistic brain networks with 84 regions (Desikan-Killiany atlas)
- No, weak, strong coupling
- 21, 42, 63 observed regions out of 84
- Each combination: two batches with 10 seizures each
- Excitabilities drawn randomly from standard normal distribution
- Random selection of observed nodes

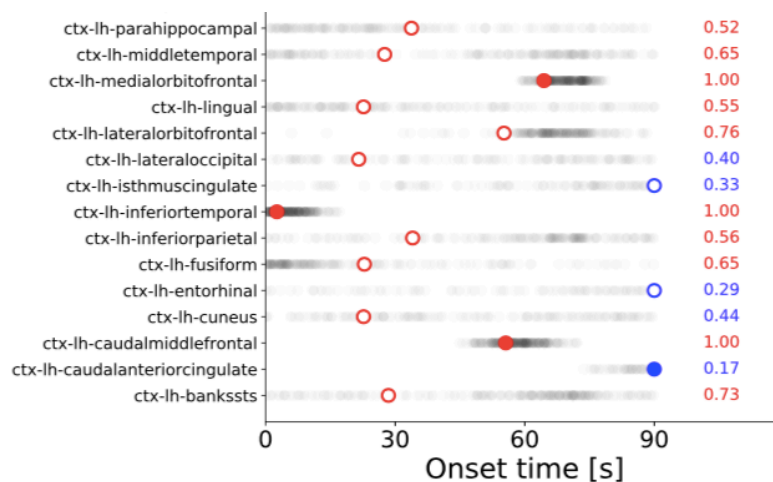
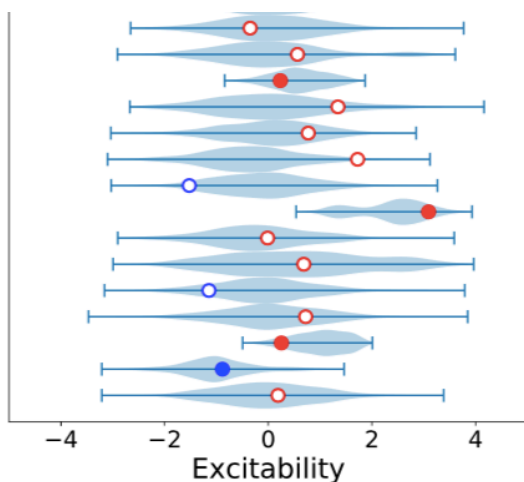
# Example

Strong coupling, 84 regions, 21 observed, 10 seizures in a batch



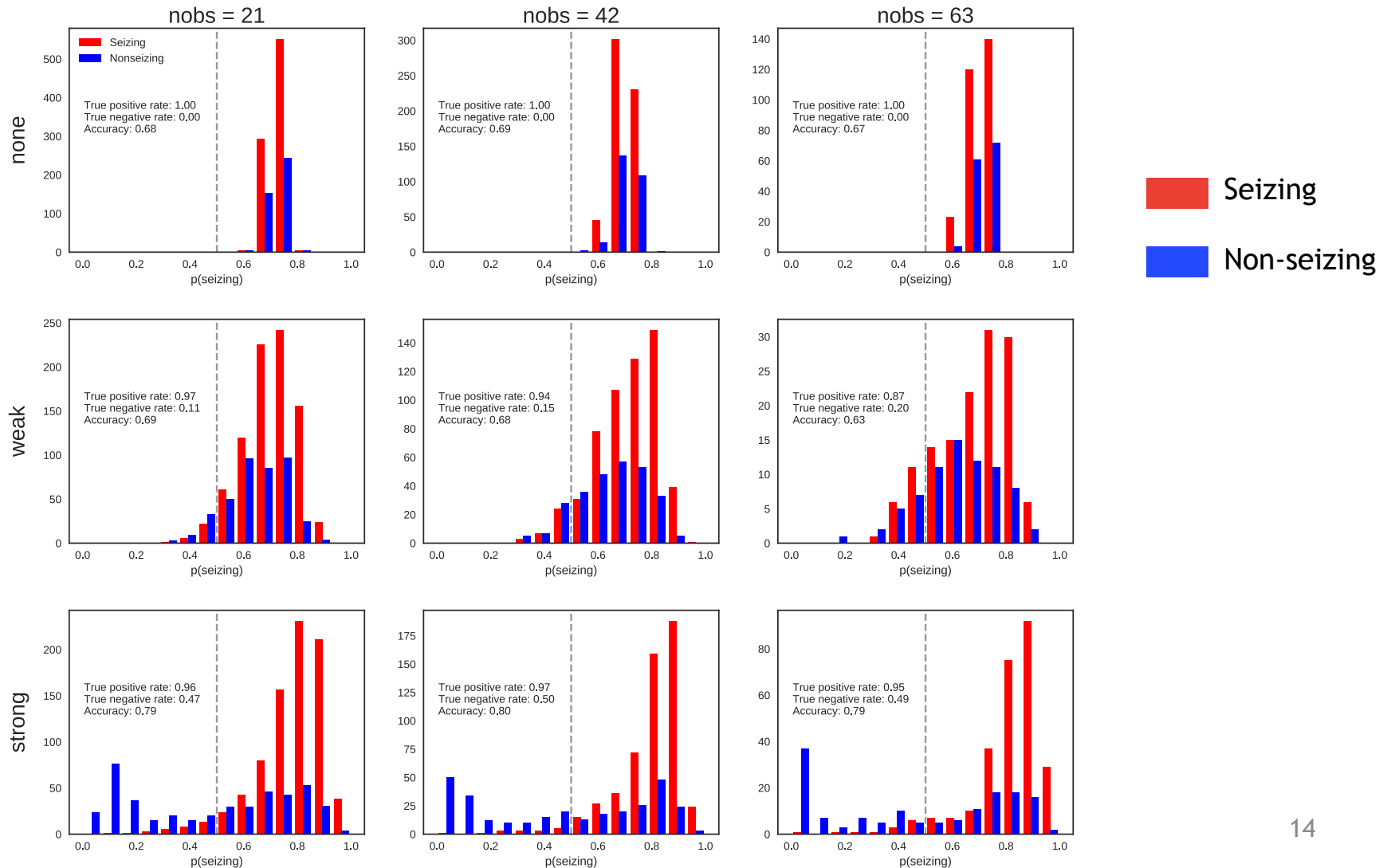
## Ground truth

- Observed seizure
- Hidden seizure
- Observed non-seizing
- Hidden non-seizing



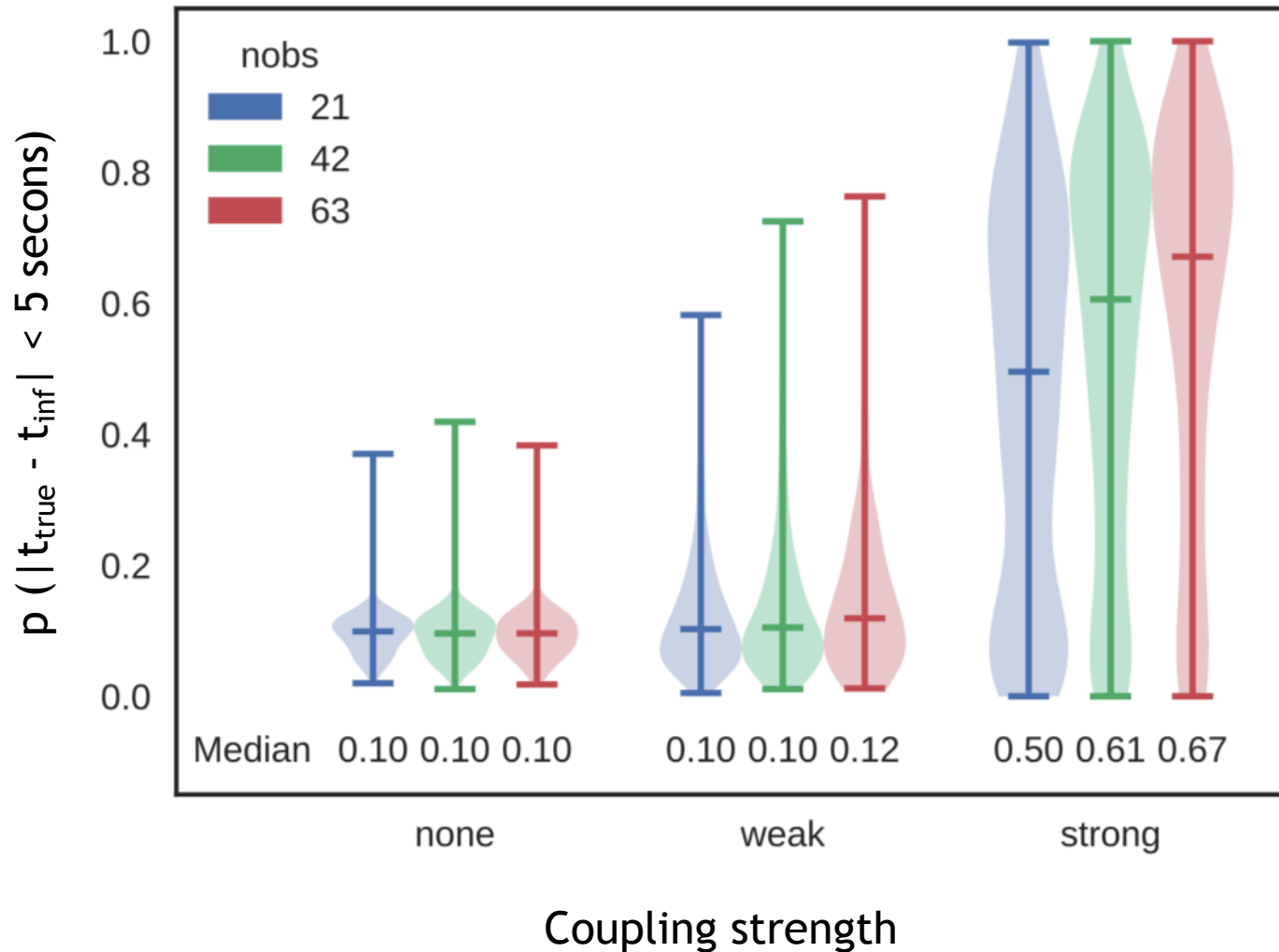
# Can we determine if a hidden region is seizing?

Number of observed regions (out of 84)



Coupling strength

# Can we determine when a hidden region starts to seize?

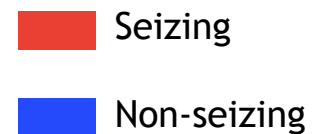
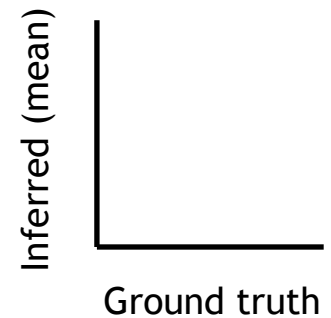
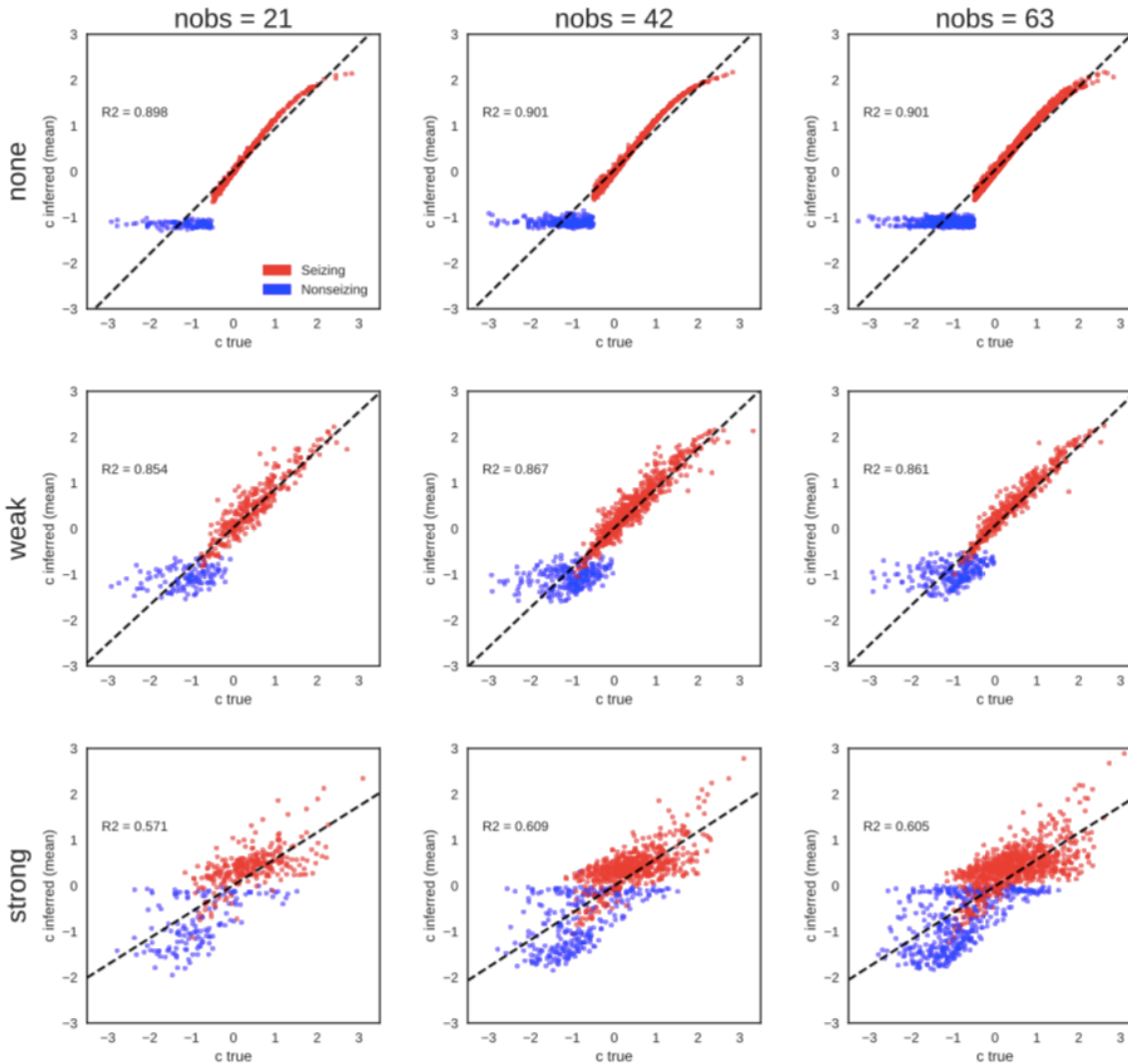


# Can we infer the excitabilities?

## Observed regions

Number of observed regions

Coupling strength



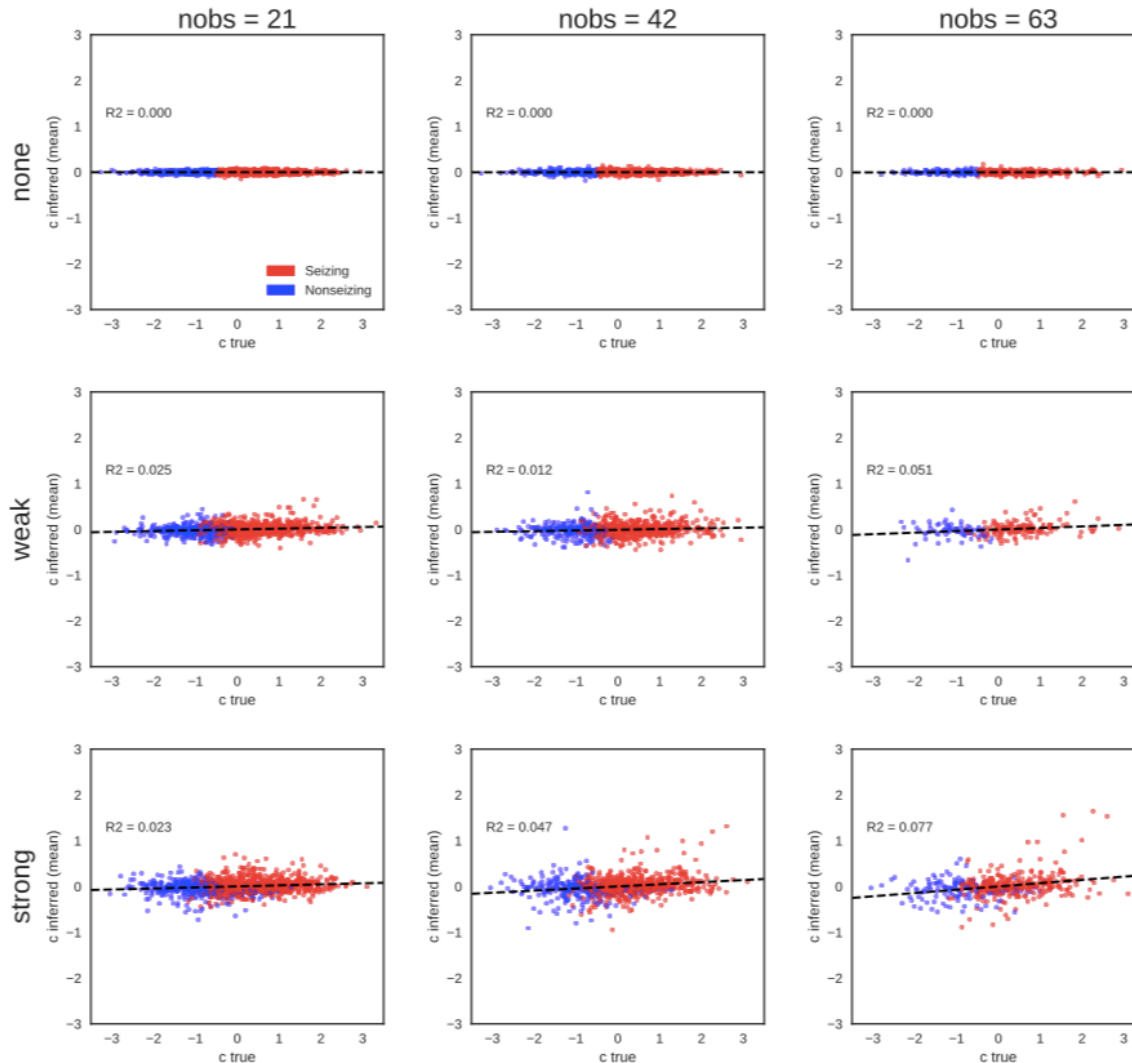


# Can we infer the excitabilities?

## Hidden regions

Number of observed regions

Coupling strength



Inferred (mean)

Ground truth

Seizing

Non-seizing

# Summary

- Simple model with minimal assumptions:
  - Binary healthy/seizure state
  - Seizure propagates along the network
  - Seizing nodes destabilize neighbours
  - Recruitment influenced by the internal excitability
- Only few constants to set:
  - Temporal scale of interest
  - Wide priors on the hyperparameters
- Simple model allows for full brain network inference for batch of subjects.
- With strong enough coupling effects, onset times in the hidden network can be in part inferred.

Institut de Neurosciences des Systèmes, AMU

**Viktor Jirsa**

Huifang Wang

Marmaduke Woodman

Meysam Hashemi

Anirudh Vattikonda

Assistance Publique - Hôpitaux de Marseille

Fabrice Bartolomei

Center for Magnetic Resonance in Biology and  
Medicine, AMU

Maxime Guye

- This research has received funding from the European Union's Horizon 2020 Framework Programme for Research and Innovation under the Specific Grant Agreement No. 785907 (Human Brain Project SGA2).
- Research supported by FRM DIC20161236442.