

# Coupled Oscillations of Calcium and IP3: Identification of Feedback Loops

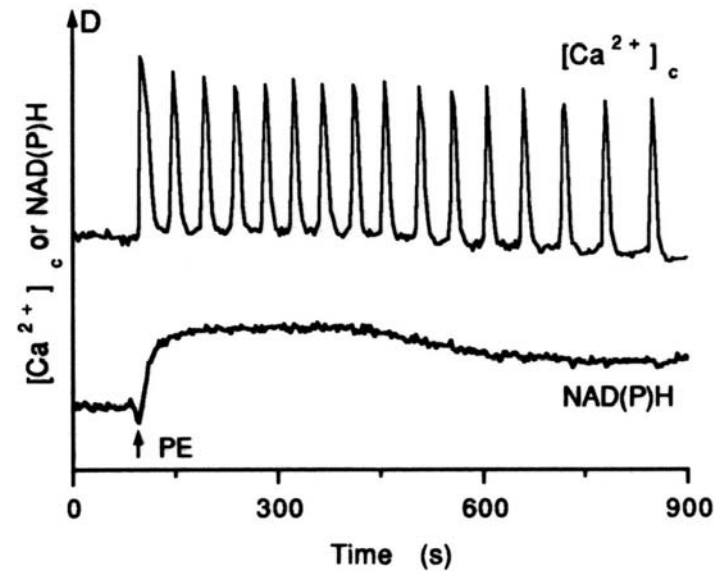
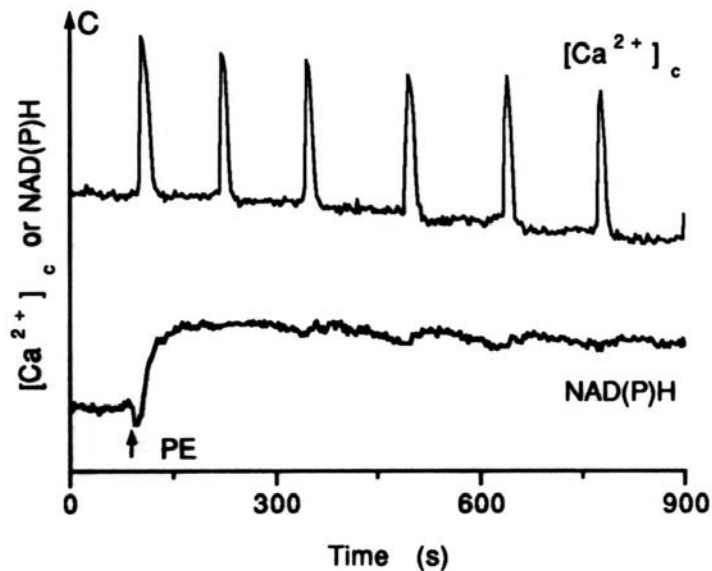
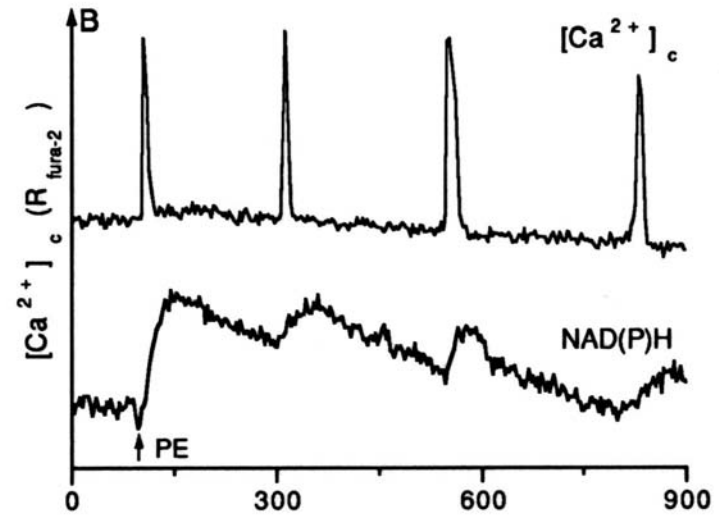
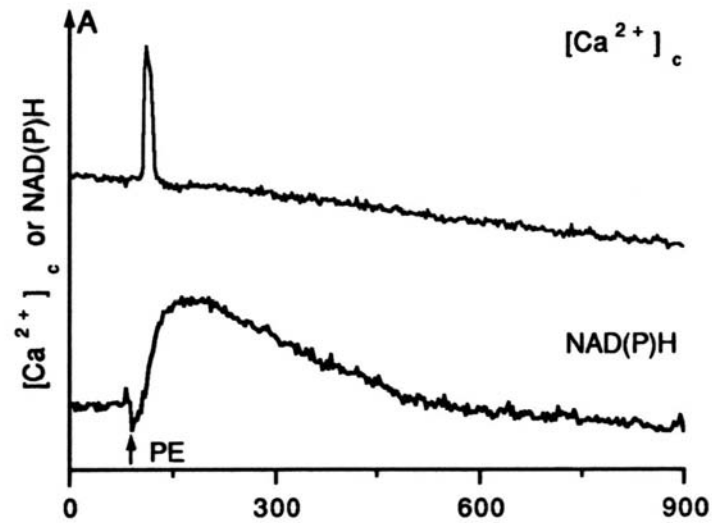


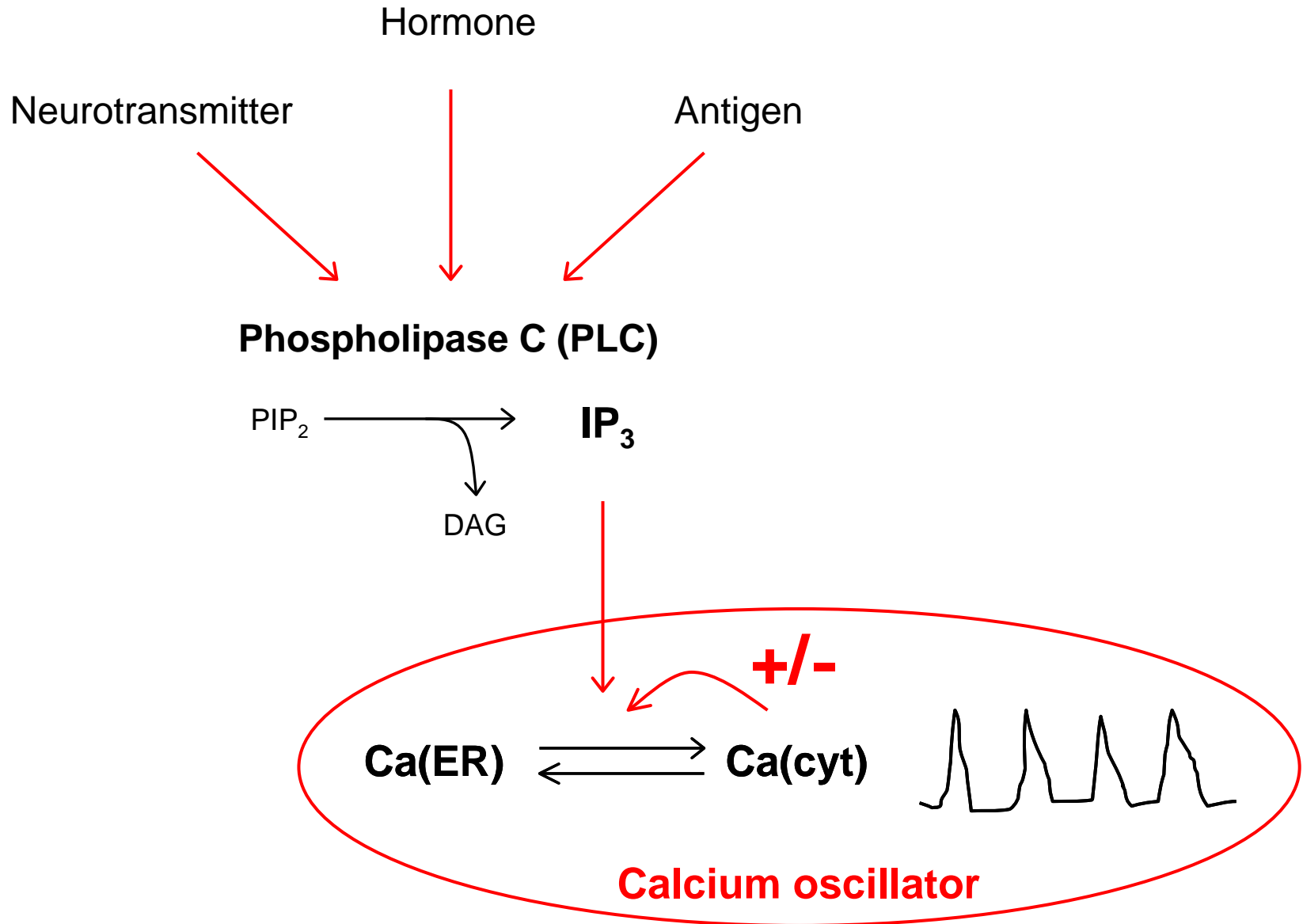
**Antonio Politi**

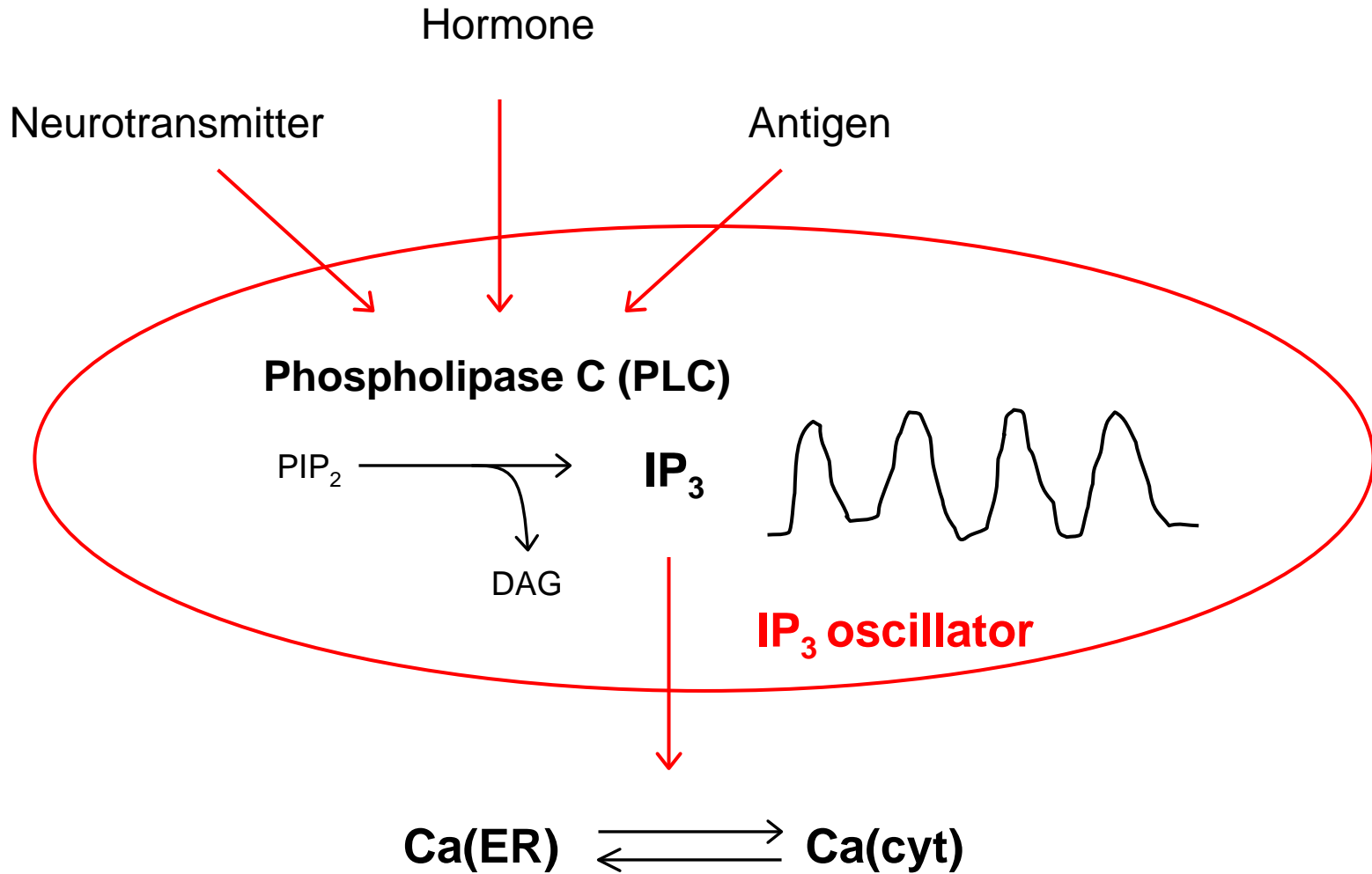


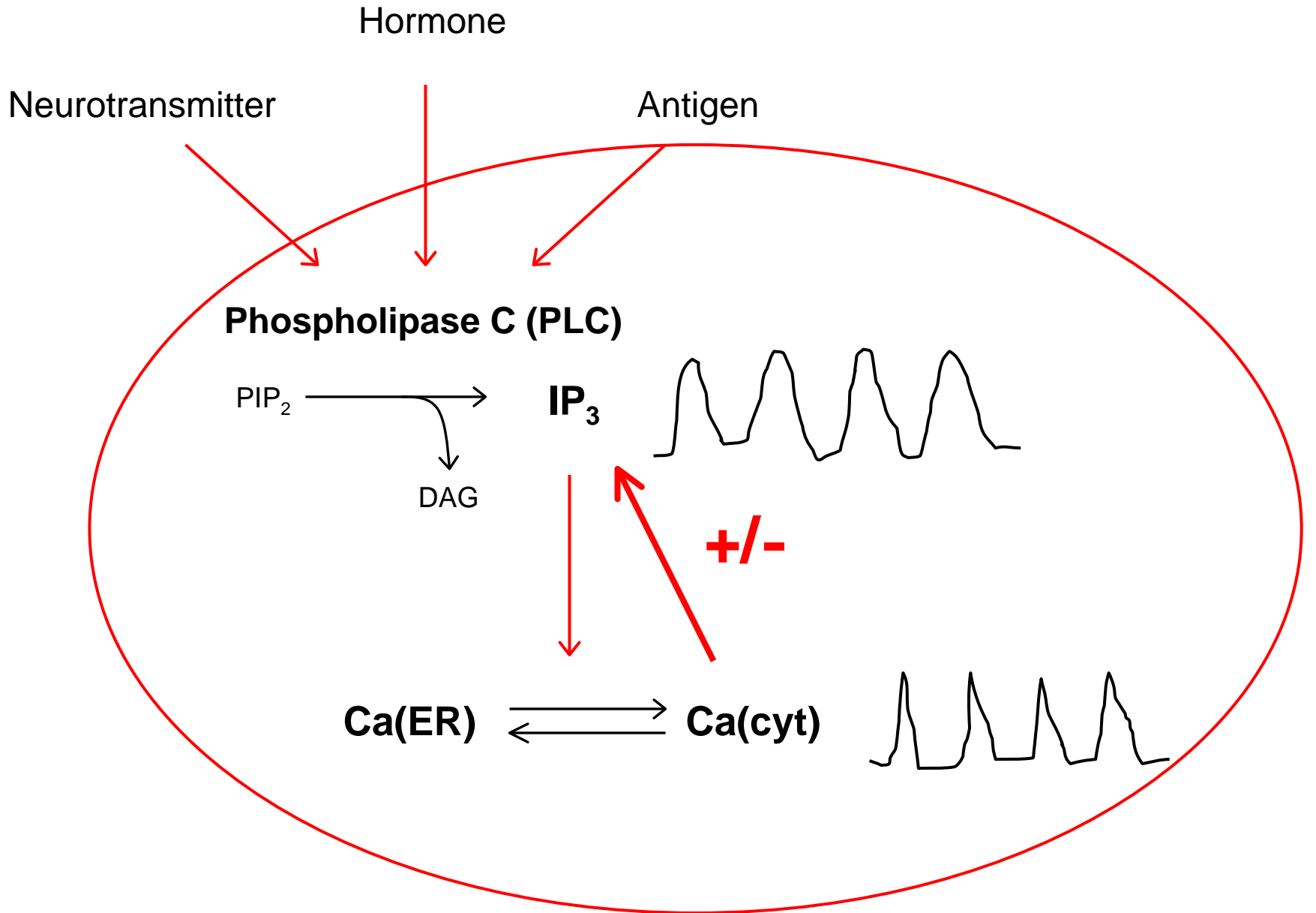
**with Andrew Thomas  
& Larry Gaspers  
New Jersey Med School**

# Frequency-modulated $\text{Ca}^{2+}$ oscillations and control of metabolism in hepatocytes









## **Ca elevates IP3**

Haratounian et al. (1991)

Venance et al. (1997)

## **Models for Ca/IP3 wave propagation**

Höfer, Venance and Giaume (2002)

Dupont and Dummollard (2004)

Wagner et al. (2004)

## **Models with IP3 oscillations**

Meyer and Stryer (1988)

Cuthbertson and Chay (1991)

Kummer et al. (2000)

Dupont and Erneux (1997)

Dupont et al. (2003)

## **Experiment: IP3/PIP2 oscillate**

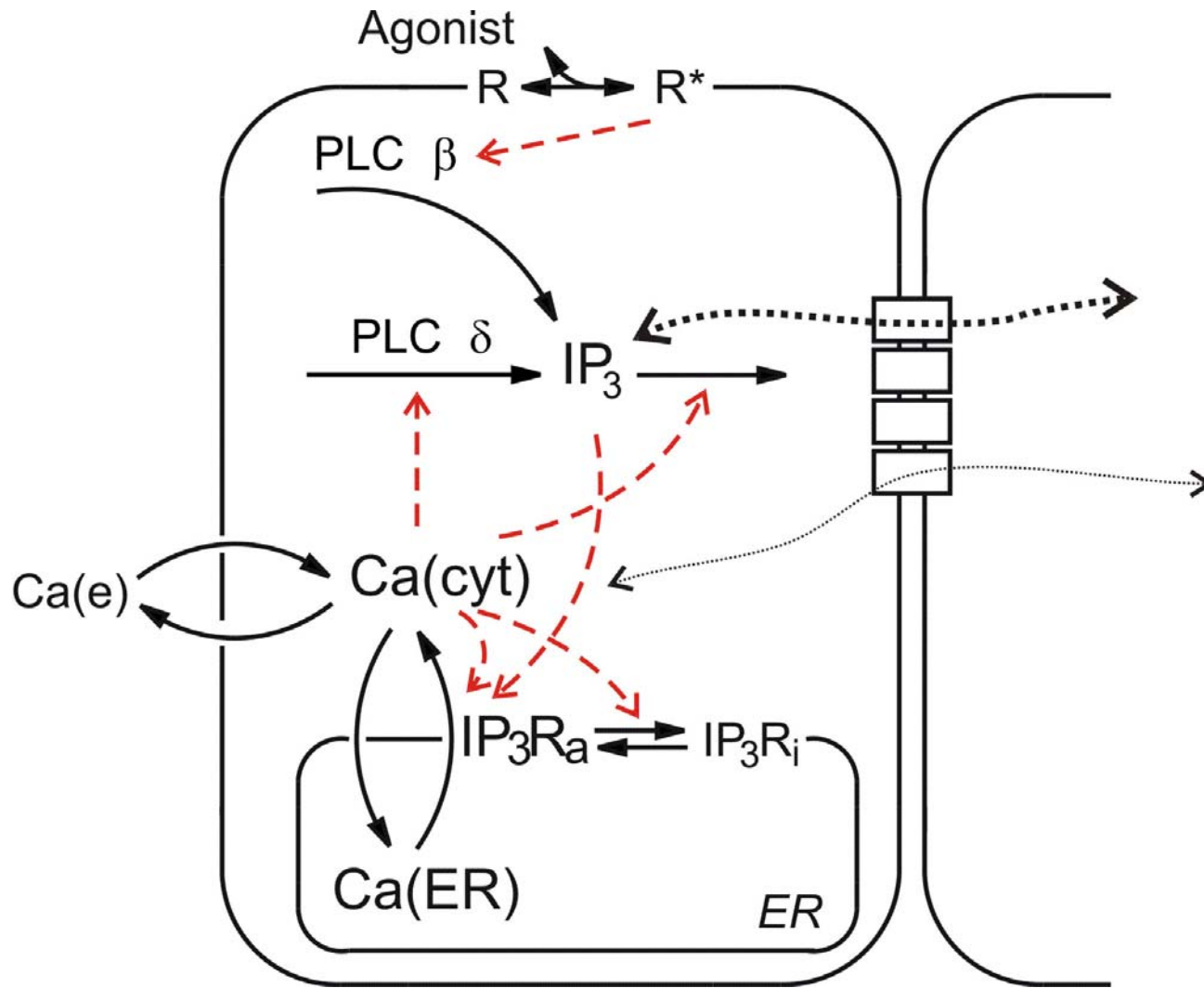
Hirose et al. (1999)

Nash et al. (2000)

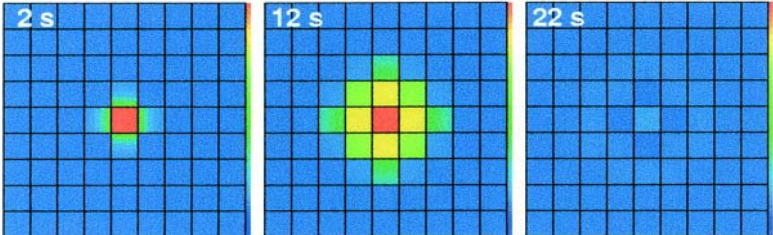
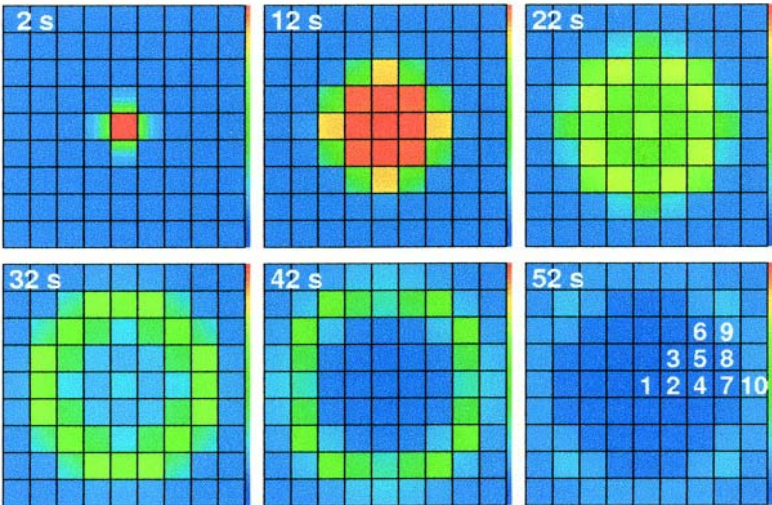
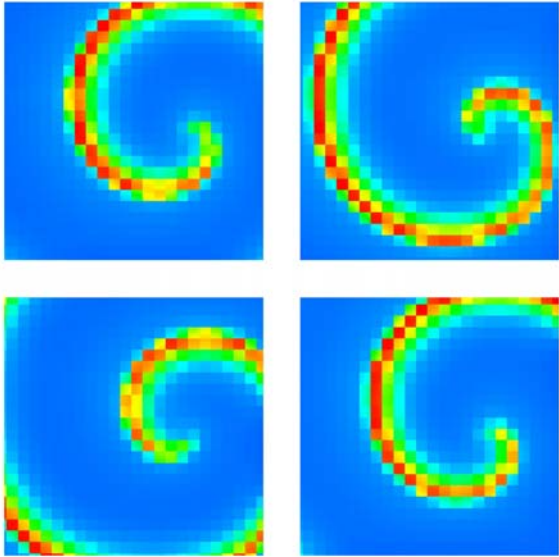
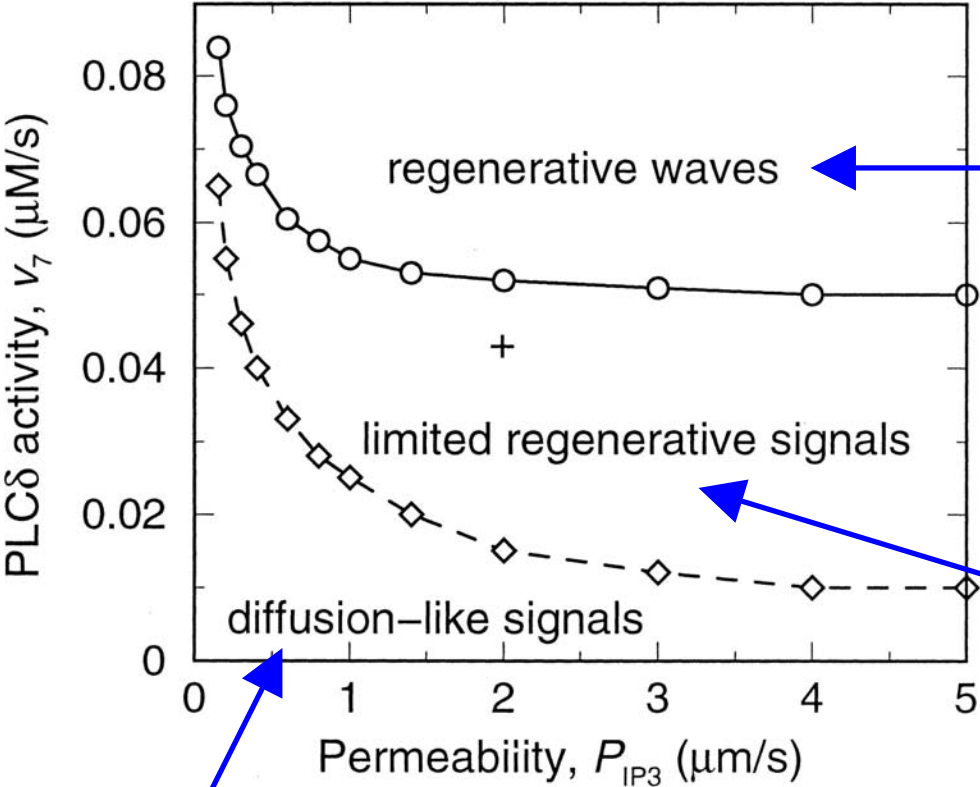
Young et al. (2003)

Thore et al. (2004)

**Is dynamic IP3 essential for the calcium oscillator?**

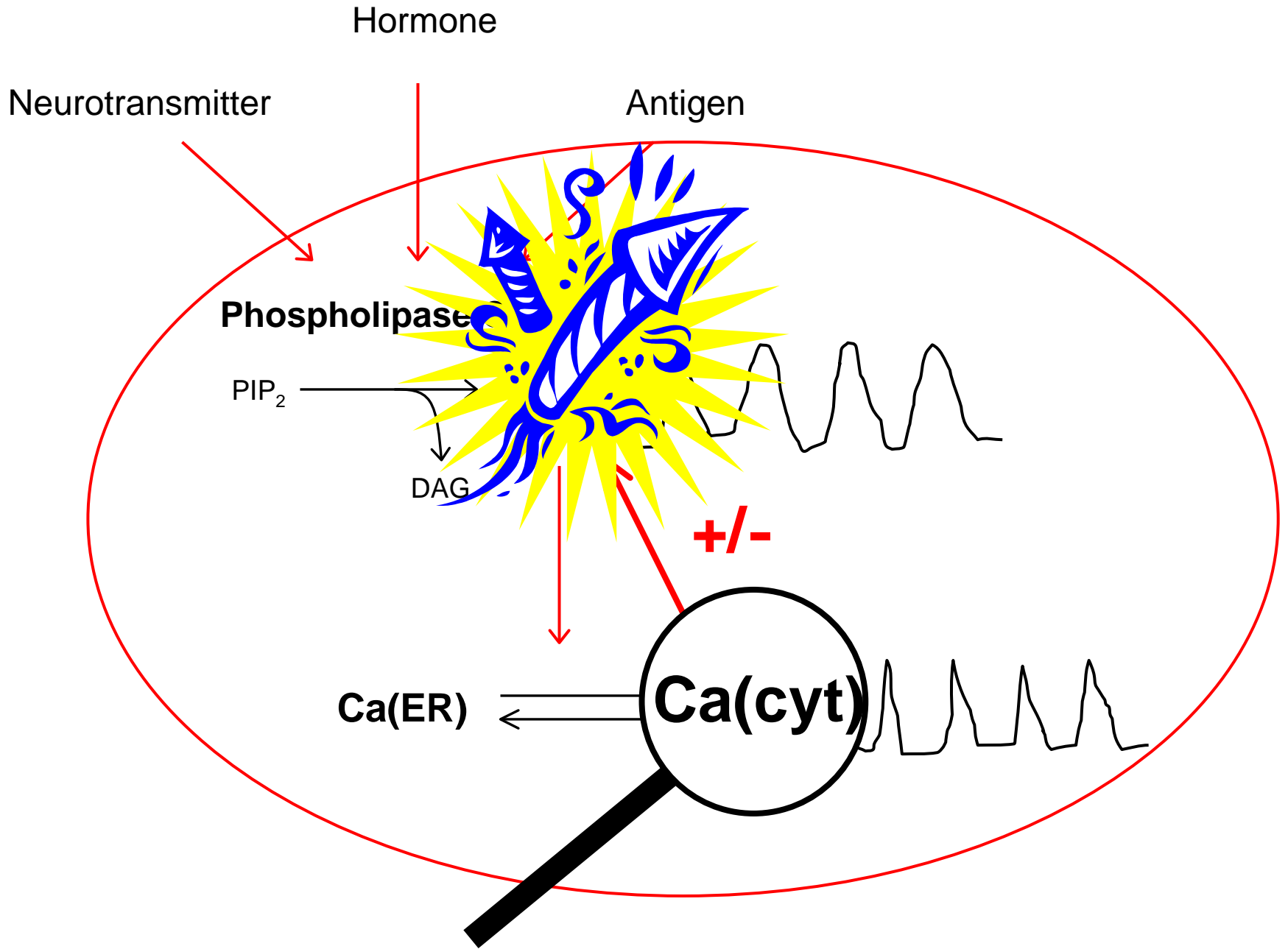


# 3 modes of intercellular signaling



6 9  
3 5 8  
1 2 4 7 10



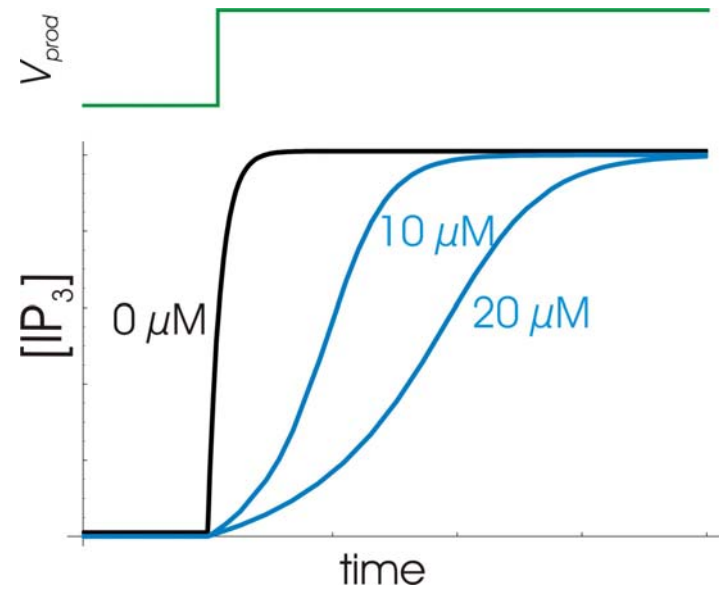


# Slowing IP3 turnover with a buffer protein

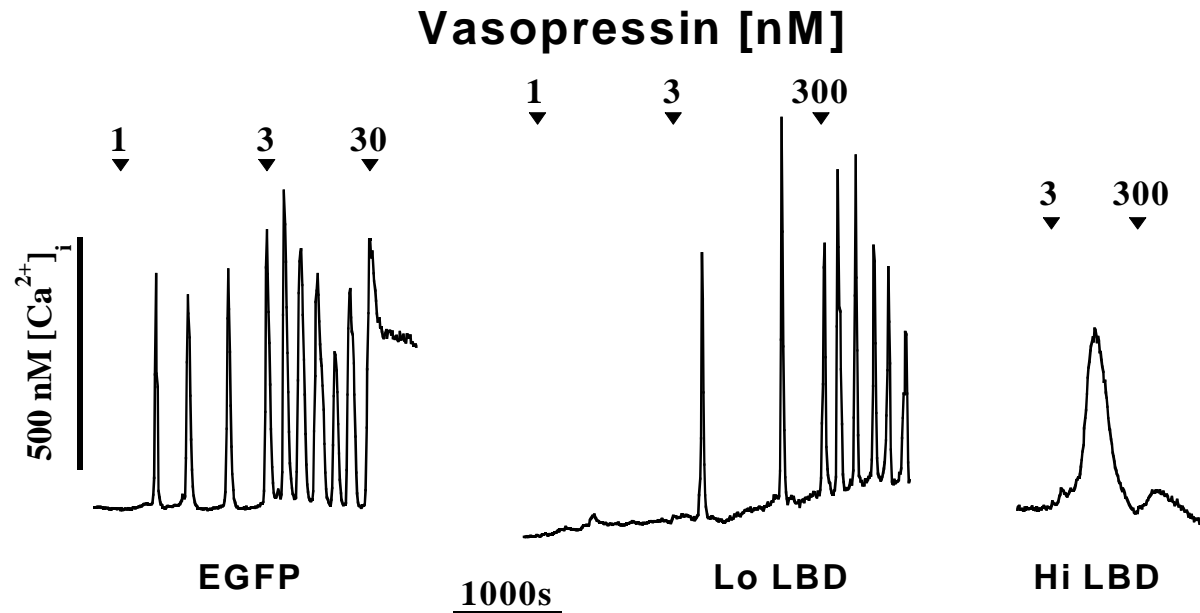


$$\frac{d[IP_3]}{dt} = \frac{1}{\tau_P} (V_{prod} - V_{deg})$$

$$\tau_P = \frac{1}{k_P} \left( 1 + \frac{K_d B_T}{(K_d + [IP_3])^2} \right)$$



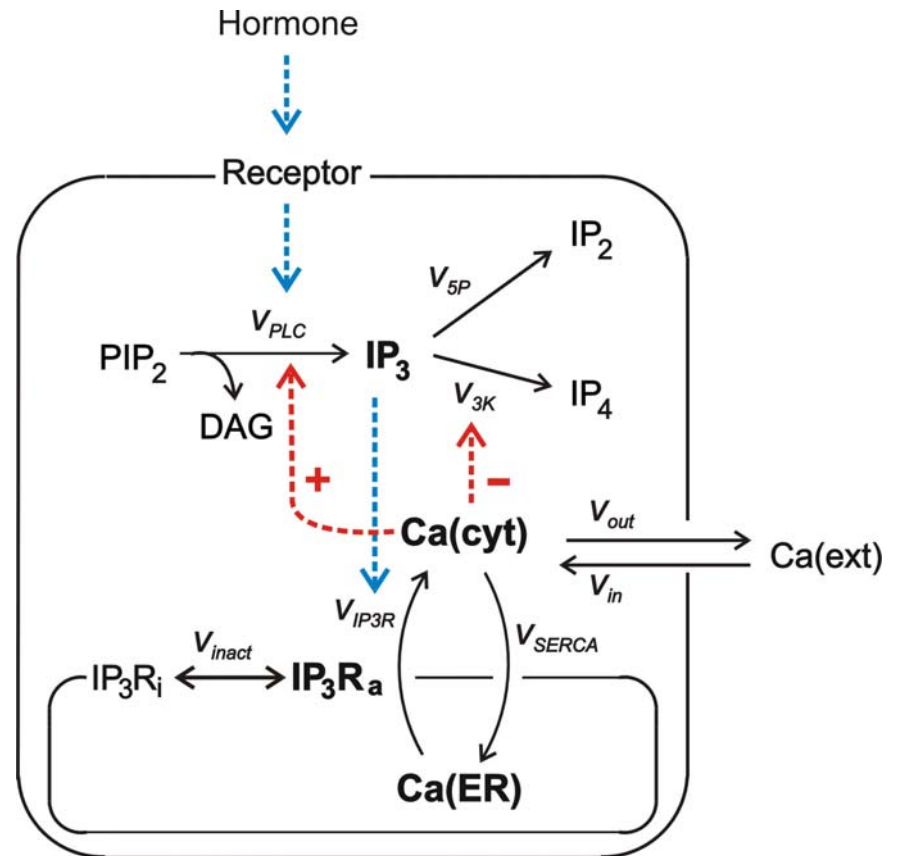
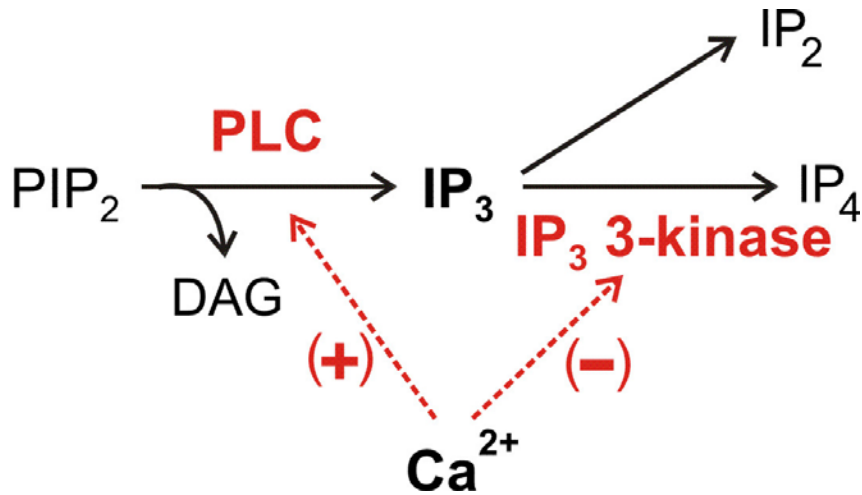
# Response to IP3 buffer in hepatocytes



**How are IP3 oscillations mediated?**

**Do they serve a function?**

# Negative and positive feedbacks of calcium on IP3



## Ca<sup>2+</sup> activation of PLC

$$\frac{dp}{dt} = \frac{1}{\tau_p} \left[ V_{PLC,1} + V_{PLC,2} \frac{c^2}{K_{PLC}^2 + c^2} - p \right]$$

**Ca activation**

$$\frac{dc}{dt} = \frac{1}{\tau_c} \left[ \left( \frac{(rpc)^3}{(K_p + p)^3 (K_a + c)^3} + k_2 \right) (c_{ER} - c) - v_S \frac{c^2}{K_S^2 + c^2} \right]$$

$$\frac{dr}{dt} = \frac{1}{\tau_r} [1 - (1 + c/K_i)r]$$

$$W_C c + W_{ER} c_{ER} = n_{tot}$$

## Ca<sup>2+</sup> activation IP<sub>3</sub> 3-kinase

$$\frac{dp}{dt} = \frac{1}{\tau_p} \left[ v_{PLC,1} - \left( 1 - \eta + \eta \frac{c^2}{K_{3K}^2 + c^2} \right) p \right], \quad 0 \leq \eta \leq 1$$

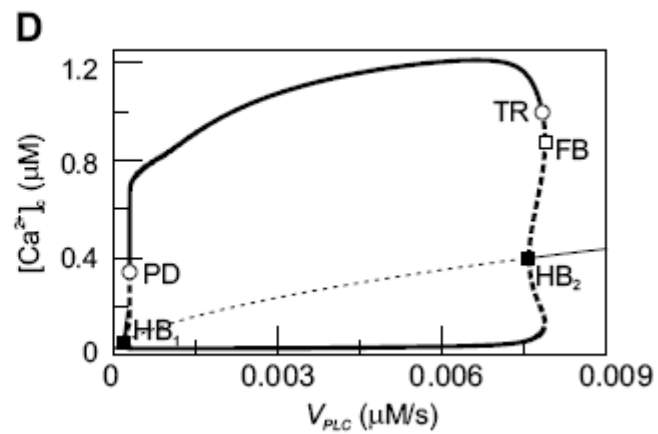
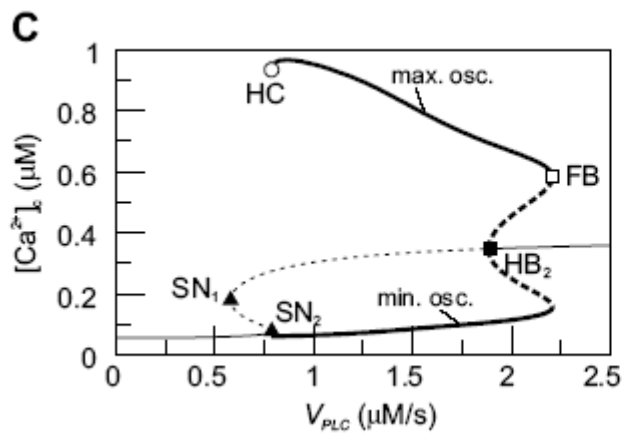
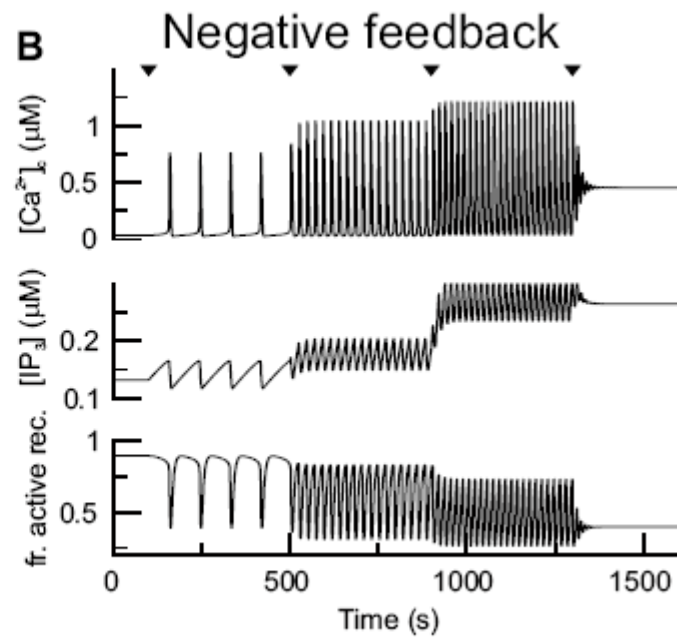
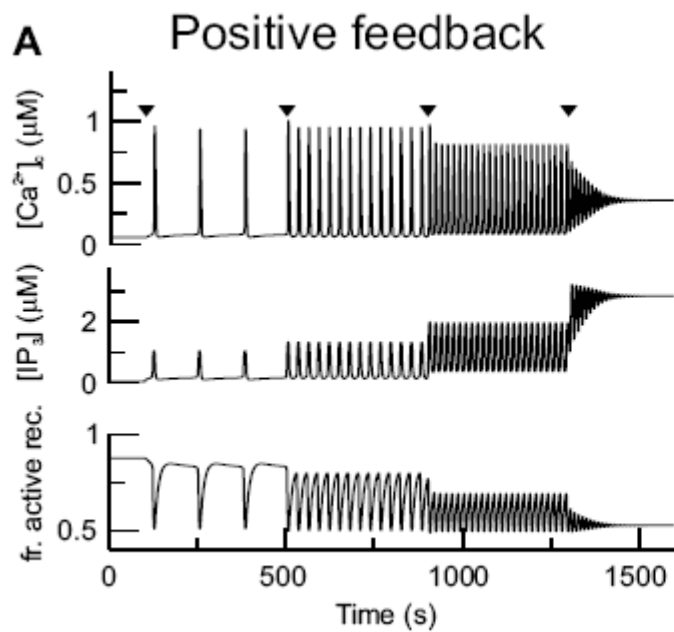
Ca activation

$$\frac{dc}{dt} = \frac{1}{\tau_c} \left[ \left( \frac{(rpc)^3}{(K_p + p)^3 (K_a + c)^3} + k_2 \right) (c_{ER} - c) - v_S \frac{c^2}{K_S^2 + c^2} \right]$$

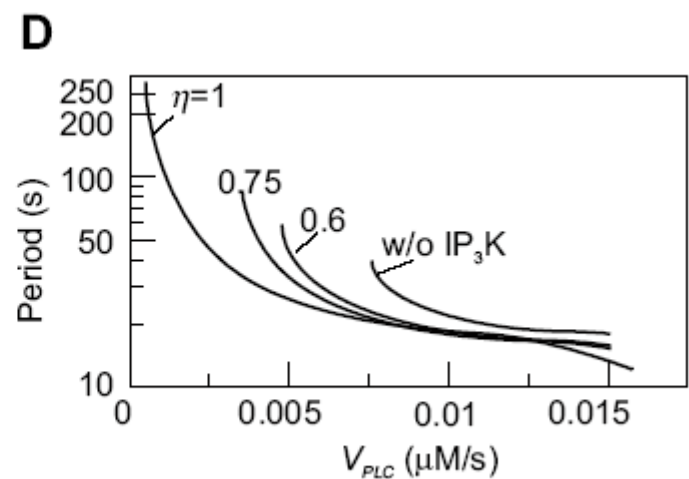
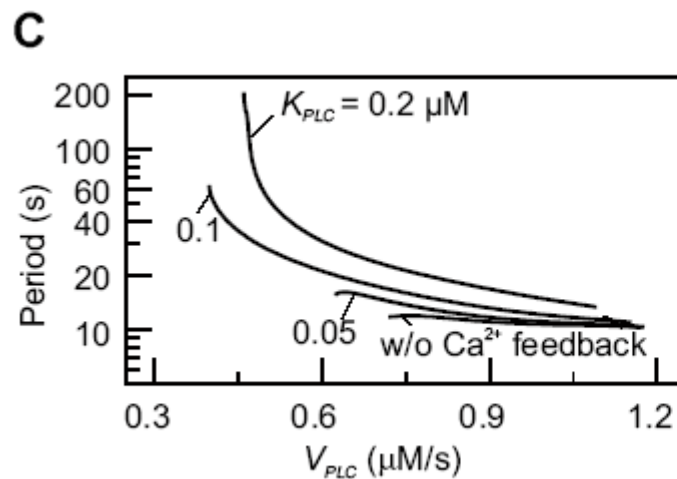
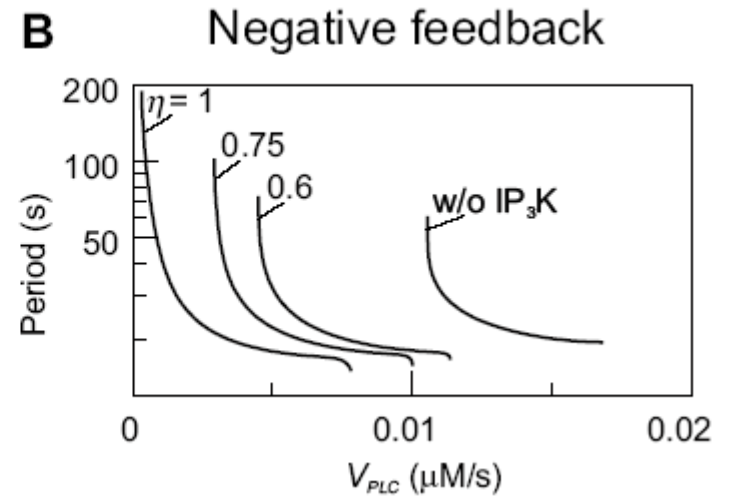
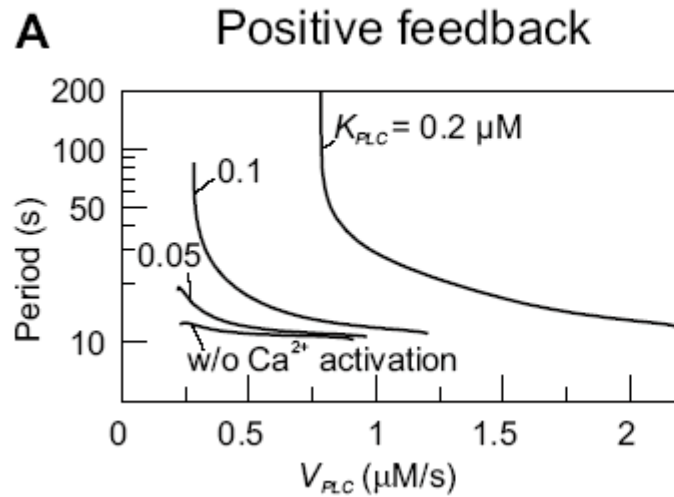
$$\frac{dr}{dt} = \frac{1}{\tau_r} [1 - (1 + c/K_i)r]$$

$$W_C c + W_{ER} c_{ER} = n_{tot}$$

Agonist

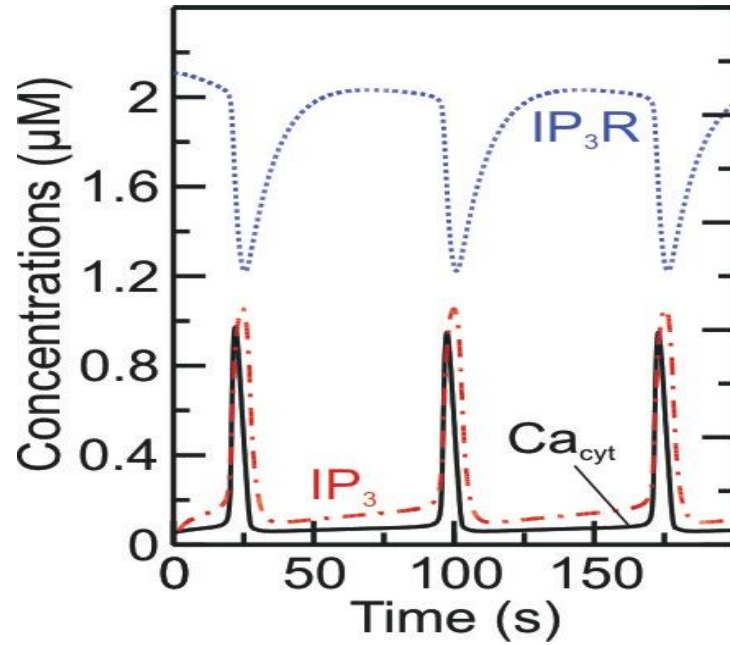


# Feedbacks support frequency encoding of hormone dose

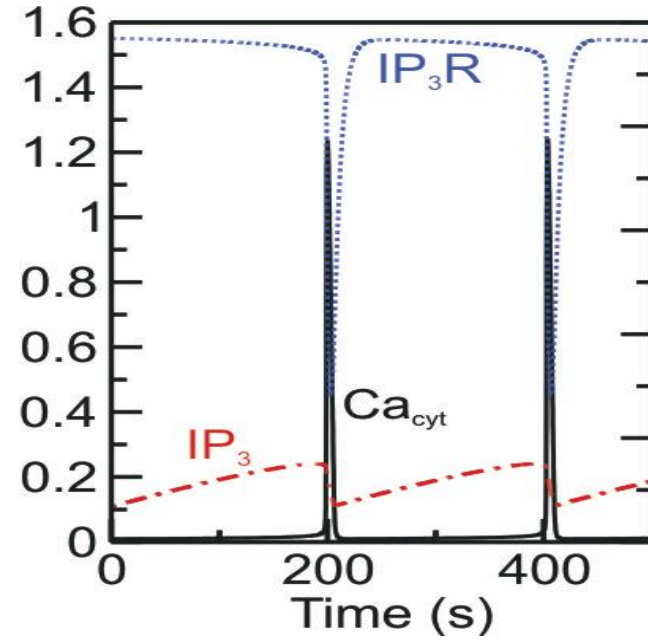




## Positive feedback

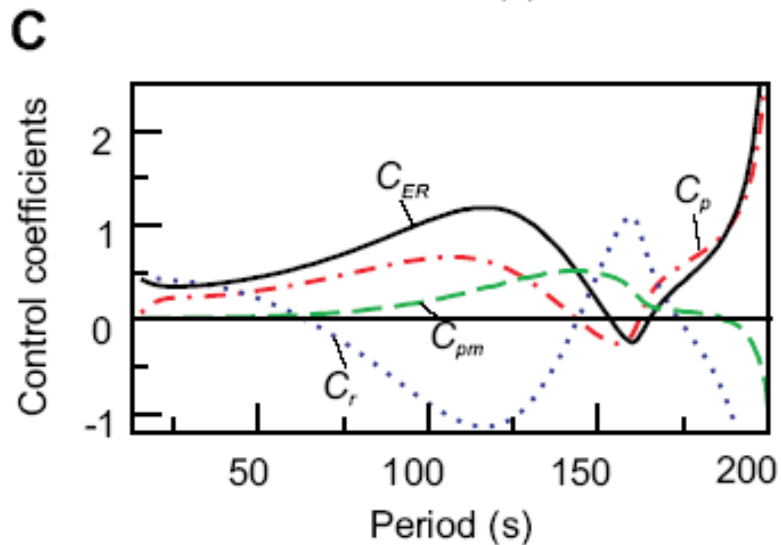
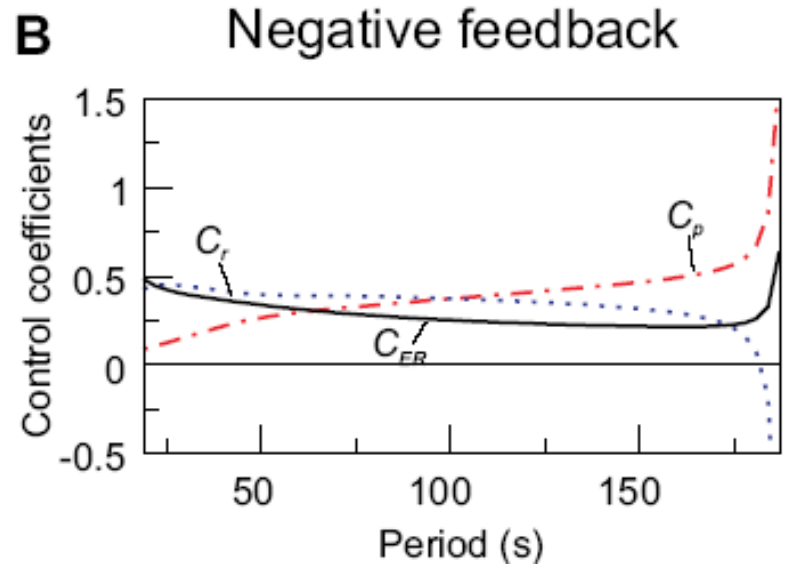
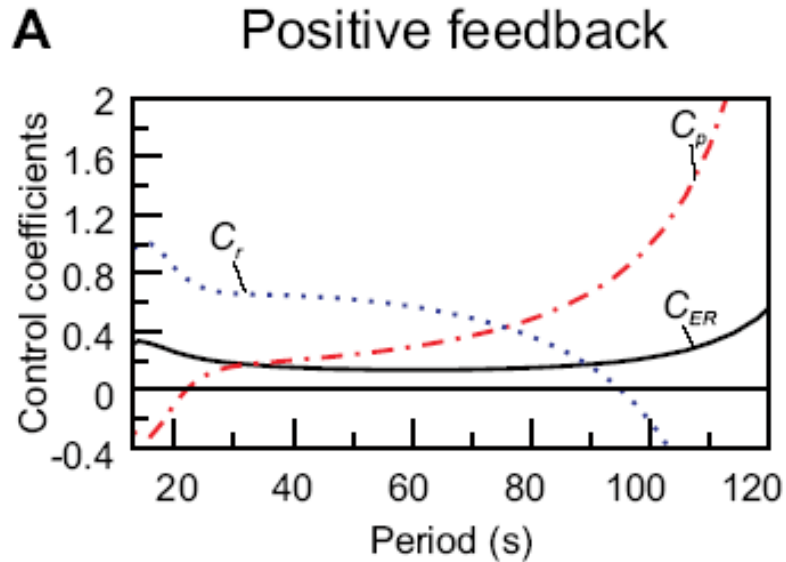


## Negative feedback



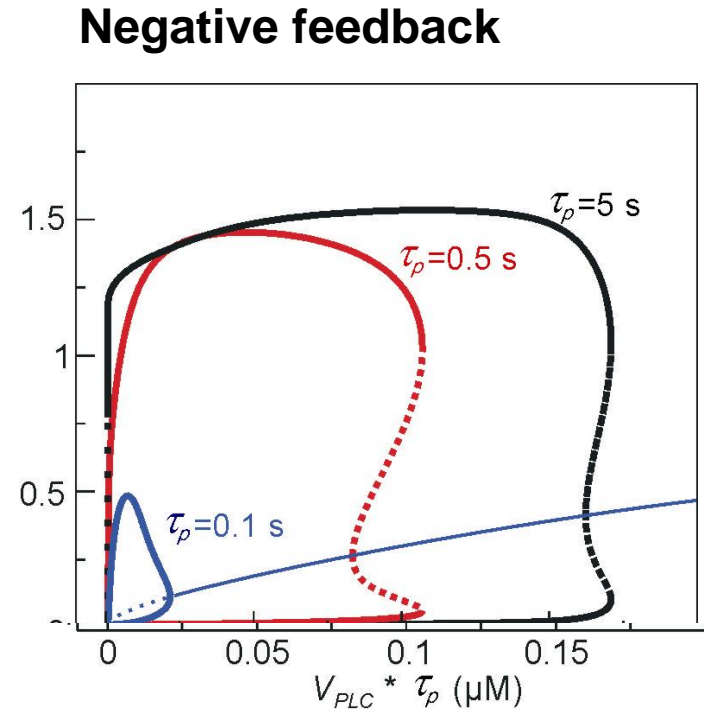
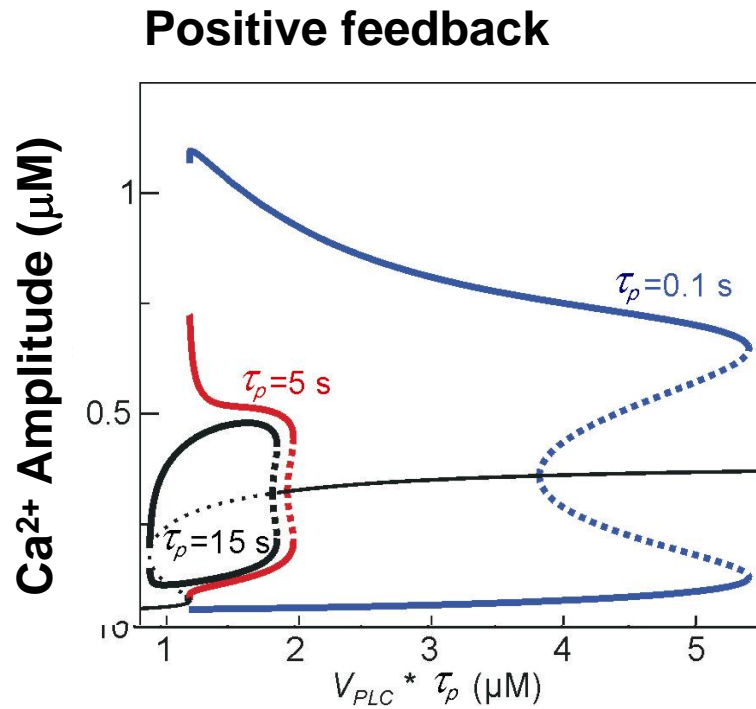
## Period control

$$C_i^T = \frac{\partial \ln T}{\partial \ln \tau_i}$$



With  $\text{Ca}^{2+}$   
PM fluxes

# Sensitivity to IP3 turnover differs

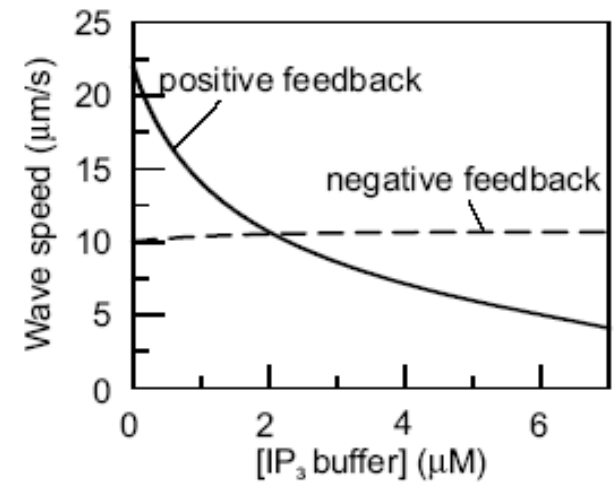
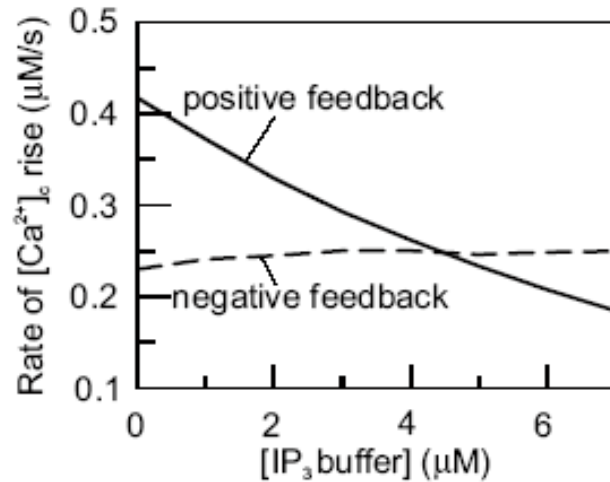


Agonist stimulus  $\longrightarrow$

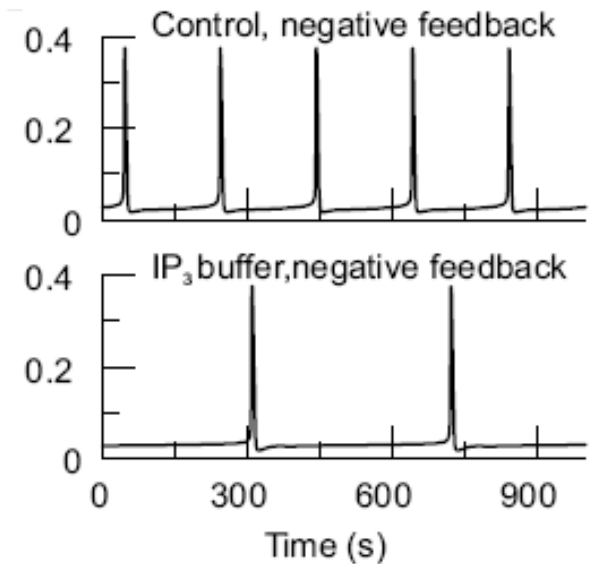
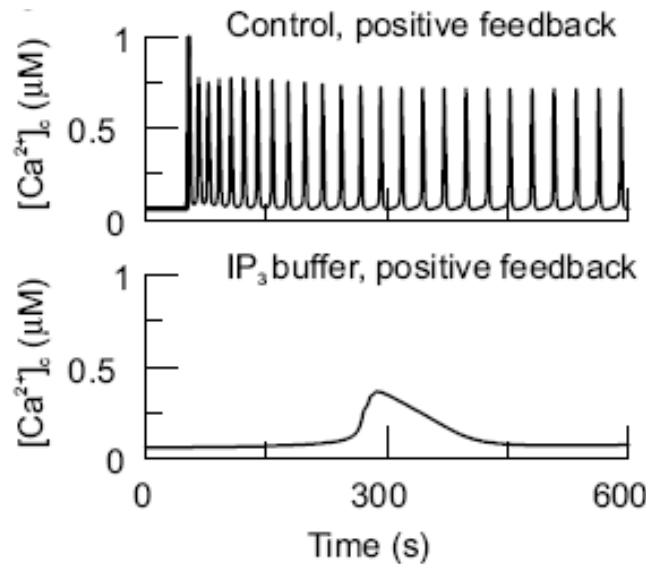
Range of oscillations for **fast**, **intermediate**, **slow** IP<sub>3</sub> turnover

# IP<sub>3</sub> buffer affects Ca<sup>2+</sup> oscillations differently in the positive and negative feedback models

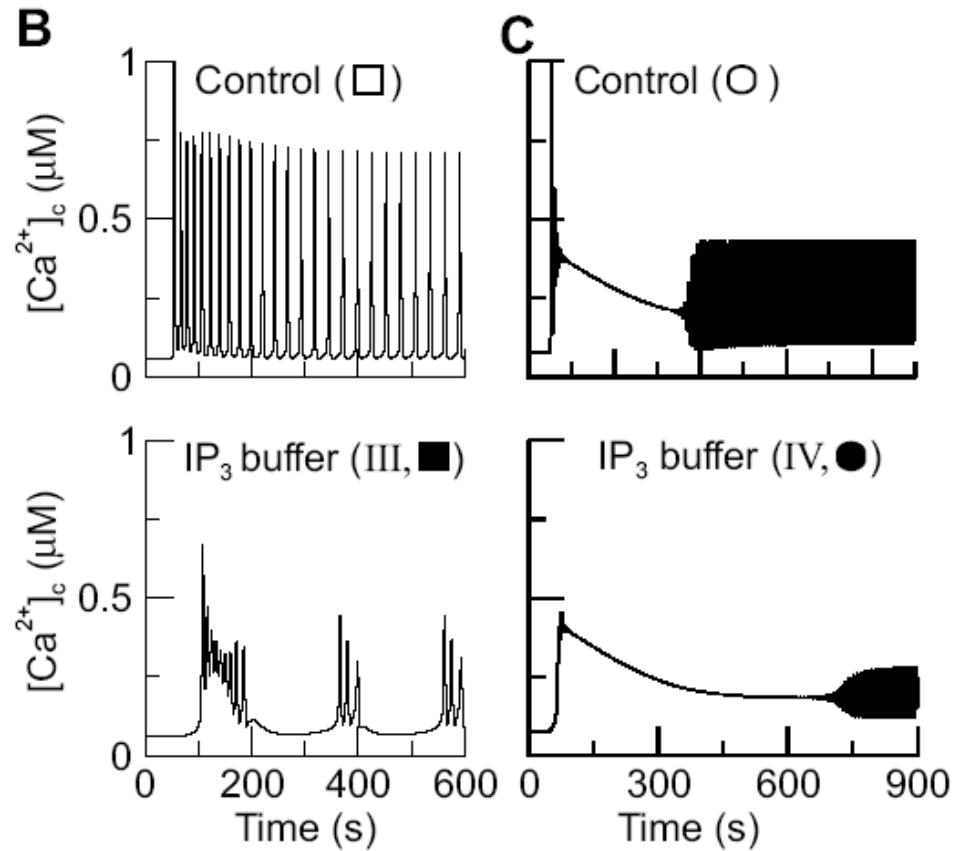
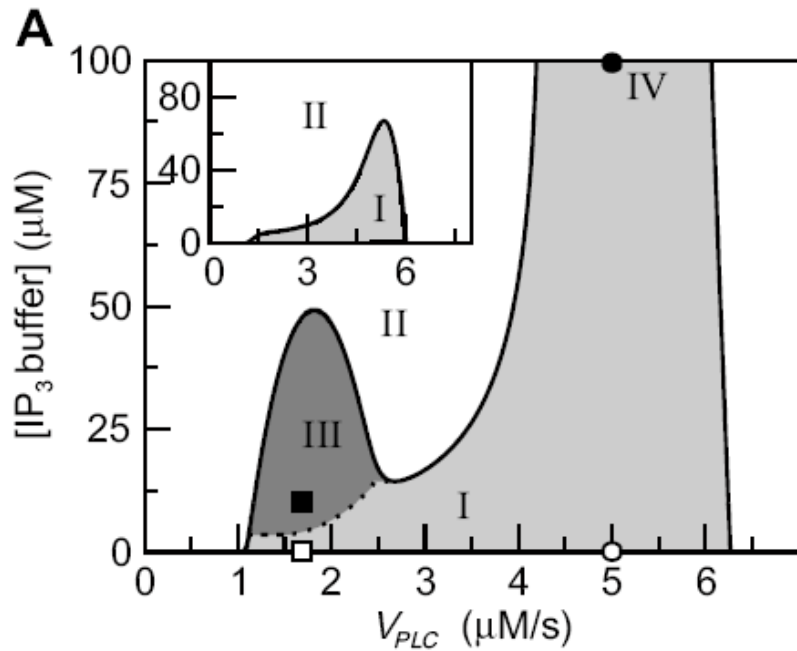
Low IP<sub>3</sub> buffer



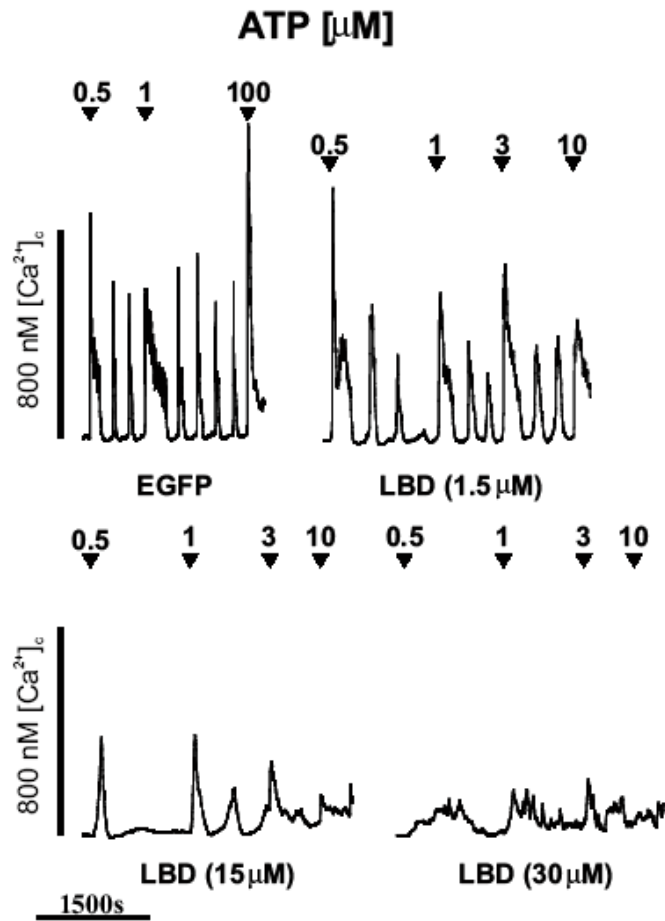
High IP<sub>3</sub> buffer



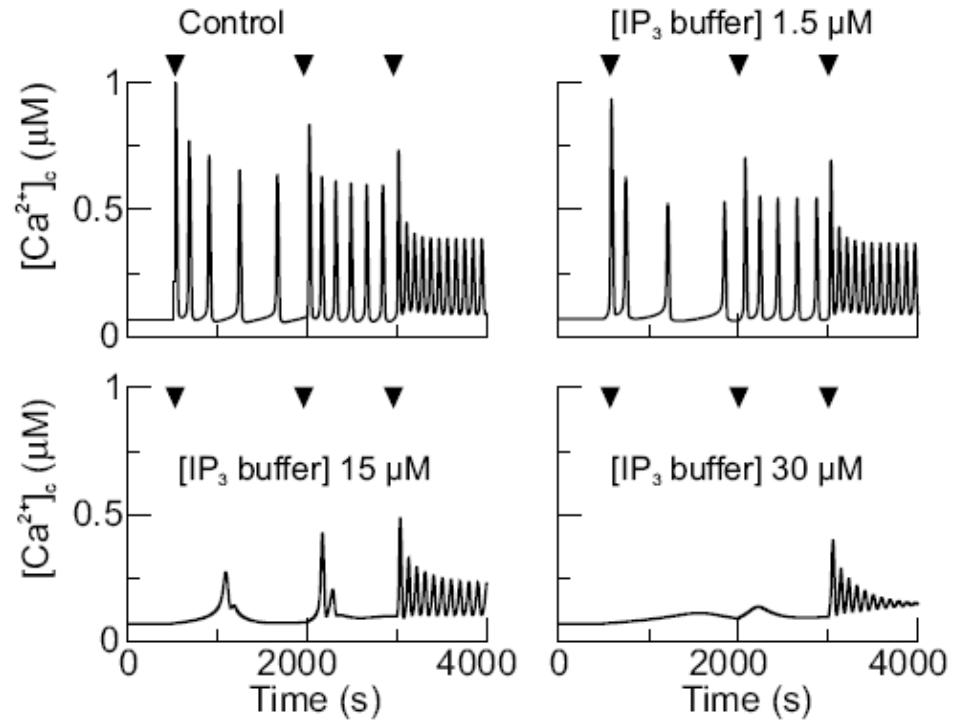
# Complex buffer effects



## Experiment 3 – CHO cells



## Model (+ve feedback, strong PM fluxes)



# Rate of calcium rise depends on IP3 buffer

